

# Wed. Feb. 28, 2018

- **Reminder: Midterm exam next Wednesday**
  - Closed book, Closed Notes
  - Do bring a calculator
  - Review session Monday
- **Today:**
  - Finish Thermal Remote Sensing Pt. 1 (IR emission)
    - Use Monday's posted slides
- **Today + Friday:**
  - Thermal Remote Sensing Pt. 2 (Heat transfer)
    - New slides posted for today
- **Tomorrow at ~3PM MST: Launch of GOES-S**
  - NASA TV or <<http://www.spaceflightnow.com>>

# GOES-S Launch Tomorrow



- 2nd of 4 in upgraded “GOES-R” series
  - First GOES-R (now GOES-16) launched Nov. 2016
  - Will be renamed GOES-17 once in operation
  - To be positioned at 137° W Long. (Pacific Coast)
    - GOES-16 is positioned off East Coast
  - 15 year expected life
- Geosynchronous (equatorial) satellites like this launch from Cape Canaveral
  - (POES launch from Vandenberg on W. Coast)
  - 2 hr launch window opens as 3:02 MST
  - Coverage on NASA TV and <<http://spaceflightnow.com>>



Use slides posted Monday  
for first part (Thermal Emission)

# Heat Transfer -- Today and Friday

- Thermal Remote Sensing Part 2.
  - Review -- emissivity effects
  - Temperature changes:
    - conductivity, heat capacity, diffusivity
    - thermal inertia
  - Geological Examples
  - Heat loss studies

# Heat Transfer

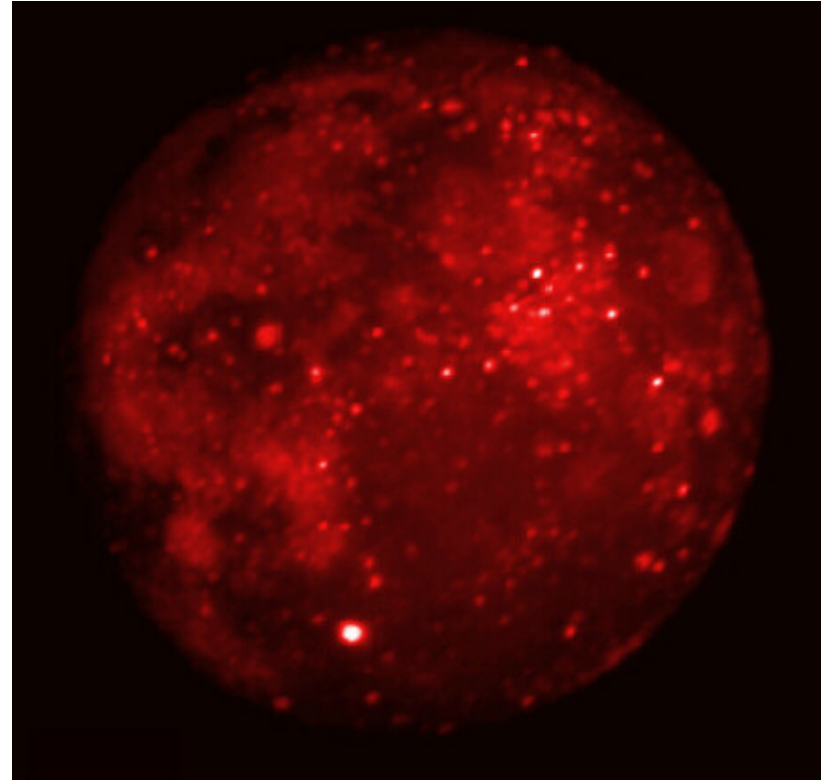
- Heat Transfer (more quantitative than Sabins)
  - Properties which control how material heats up and cools down:
    - Conductivity
    - Heat Capacity
    - Density
    - (Also albedo -- since it controls absorption of sunlight)
  - Derived terms:
    - Thermal Inertia
    - Thermal Diffusivity
    - Apparent thermal inertia

# Lunar Eclipse

## Measurements of Thermal Inertia



Visible image of full moon

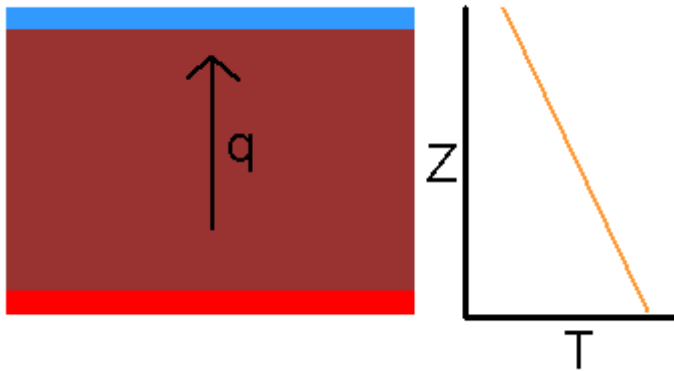


Infrared (MSX) image in eclipse

Most of moon cools quickly: Low thermal inertia  $(k\rho c)^{1/2}$   $\Rightarrow$  porous regolith  
Around craters is cools slowly: High thermal inertia  $\Rightarrow$  exposed bare rock

# Thermal Constants: Conductivity

- Heat flow  $q$ :  $\text{W/m}^2$

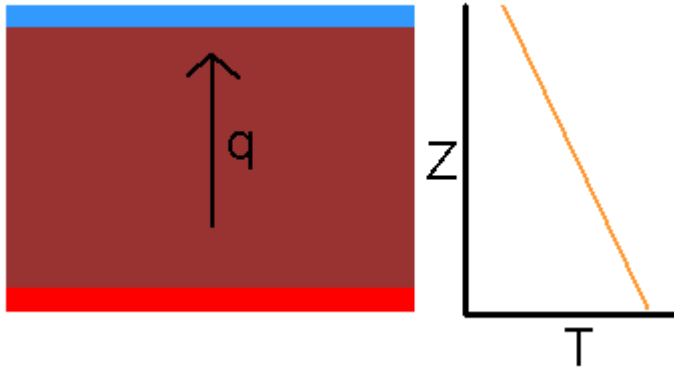


$$q = -K \frac{dT}{dz}$$

where  $K$  = Thermal Conductivity  
( $\text{W/m}^2$ )/( $\text{K/m}$ ) =  $\text{W m}^{-1} \text{K}^{-1}$

book uses “older” units of  
 $\text{cal cm}^{-1} \text{sec}^{-1} \text{ } ^\circ\text{C}^{-1}$

# Thermal Constants: Conductivity



Basalt:

$$\begin{aligned} K &= 0.0050 \text{ cal cm}^{-1} \text{ sec}^{-1} \text{ }^{\circ}\text{C}^{-1} \\ &\quad \times 4.187 \text{ J/cal} \quad \times 102 \text{ cm/m} \\ &= 2.1 \text{ J s}^{-1} \text{ m}^{-1} \text{ K}^{-1} \\ &= 2.1 \text{ W m}^{-1} \text{ K}^{-1} \end{aligned}$$

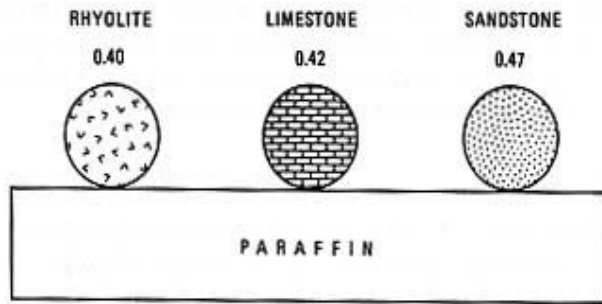
- Suppose diagram represents  $T=300\text{K}$  surface at top,  $T=1300\text{K}$  molten lava at base, with  $0.1 \text{ m}$  thick crust of basalt between.

$$q = -K \frac{dT}{dz} = -2.1 \text{ W m}^{-1} \text{ K}^{-1} \frac{1000 \text{ K}}{0.1 \text{ m}} = -21,000 \text{ W m}^{-2}$$

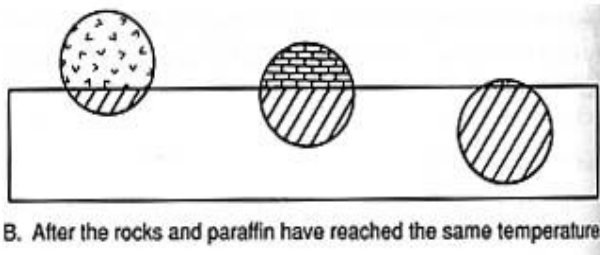
- A shoe sole is  $\sim 10 \text{ cm} \times 30 \text{ cm} = 0.1 \text{ m} \times 0.3 \text{ m} = 0.03 \text{ m}^2$  so a sole would absorb  $21,000 \text{ W m}^{-2} \times 0.03 \text{ m}^2 = 630 \text{ W}$ .  
Will get warm – but can stand it for short time.



# Heat Capacity



A. Spheres of rock heated to 100°C and placed on a sheet of paraffin. The value for each rock is the product of its thermal capacity ( $c$ ) and density ( $\rho$ ) in  $\text{cal} \cdot \text{cm}^{-3} \cdot ^\circ\text{C}^{-1}$ .



Sabins Fig. 5-4  
Amount of melt is proportional to total heat capacity

C: Heat Capacity (Thermal Capacity)  
 $\text{J kg}^{-1} \text{ } ^\circ\text{C}^{-1}$

Basalt:

$$C = 0.20 \text{ cal g}^{-1} \text{ } ^\circ\text{C}^{-1} \\ \times 4.187 \text{ J/cal} \times 1000 \text{ g/kg} \\ = 840 \text{ J kg}^{-1} \text{ K}^{-1}$$

To get heat capacity of unit volume, find  $\rho C$  where

$$\rho = \text{density} = 2.8 \text{ g cm}^{-3} \\ \times (10^2 \text{ cm/m})^3 / (10^3 \text{ g/kg}) \\ = 2800 \text{ kg m}^{-3}$$

$$\rho C = 840 \text{ J kg}^{-1} \text{ K}^{-1} \times 2800 \text{ kg m}^{-3} \\ = 2.3 \times 10^6 \text{ J m}^{-3} \text{ K}^{-1}$$

# Heating time?

Have 1 meter on a size block,  
with heat flowing into it as given in previous  
example:  $q = 21,000 \text{ W m}^{-2}$

Heat capacity per unit volume is

$$\rho C = 2.3 \times 10^6 \text{ J m}^{-3} \text{ K}^{-1}$$

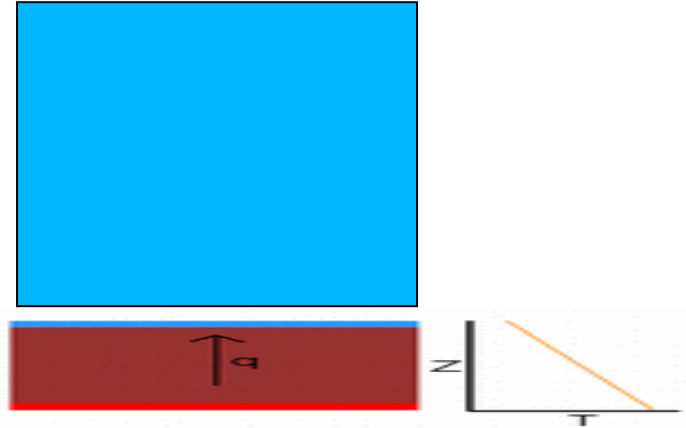
Volume is  $1 \text{ m}^3$  so total heat capacity is  $2.3 \times 10^6 \text{ J K}^{-1}$

Total heat flow is  $21,000 \text{ W} = 21,000 \text{ J s}^{-1}$   
since area  $A = 1 \text{ m}^2$ .

Heating rate will be

$$2.1 \times 10^4 \text{ J s}^{-1} / 2.3 \times 10^6 \text{ J K}^{-1} = \\ 0.91 \times 10^{-2} \text{ K s}^{-1} \sim 10^{-2} \text{ K s}^{-1}$$

Note – in above we didn't allow heat to flow out of top of  
block. Within material, heating rate will be proportional  
(heat flow in) – (heat flow out) .

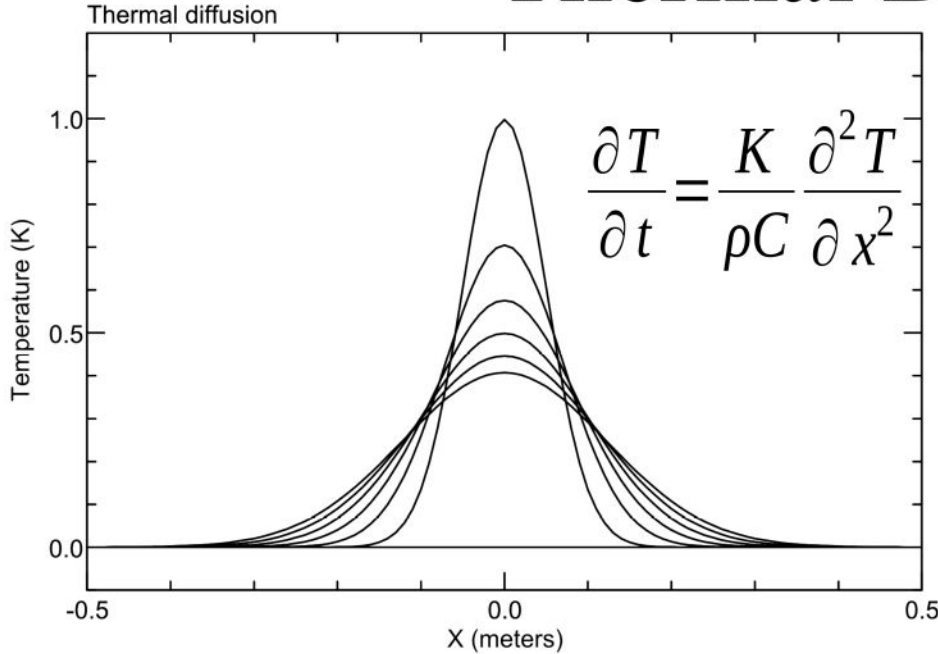


Heating rate was  
proportional to  
 $q / \rho C \propto K / (\rho C)$

Define  $k = K / (\rho C)$   
as “Thermal Diffusivity”

$$k = 2.1 \text{ W m}^{-1} \text{ K}^{-1} / \\ 2.3 \times 10^6 \text{ J m}^{-3} \text{ K}^{-1} \\ = 9.1 \times 10^{-7} \text{ m}^2 \text{ s}^{-1} \text{ for basalt}$$

# Thermal Diffusivity



How far does thermal wave propagate in given  $\Delta t$  ?  
 Assume given  $\Delta T$ , solve for  $\Delta x$ :

$$\frac{\Delta T}{\Delta t} = \frac{K}{\rho C} \frac{\Delta(\Delta T)}{(\Delta x)^2}$$

$$\Delta x = \sqrt{\frac{K}{\rho C} \Delta t}$$

For basalt  $k = 9 \times 10^{-7} \text{ m}^2 \text{ s}^{-1}$

If you wait 1 year  $= 3.15 \times 10^7 \text{ s}$ , how far does thermal wave propagate?

$$\Delta x = (9 \times 10^{-7} \text{ m}^2 \text{ s}^{-1} \times 3.15 \times 10^7 \text{ s})^{1/2} = (28 \text{ m}^2)^{1/2} = 5.3 \text{ m}$$

With sandy soil  $k = 3 \times 10^{-7} \text{ m}^2 \text{ s}^{-1}$  so

$$\Delta x = (3 \times 10^{-7} \text{ m}^2 \text{ s}^{-1} \times 3.15 \times 10^7 \text{ s})^{1/2} = (9.4 \text{ m}^2)^{1/2} = 3.1 \text{ m}$$

If you wait 1 day  $= 8.6 \times 10^4 \text{ s}$ , how far does thermal wave propagate in sandy soil?

$$\Delta x = (3 \times 10^{-7} \text{ m}^2 \text{ s}^{-1} \times 8.6 \times 10^4 \text{ s})^{1/2} = (2.6 \times 10^{-2} \text{ m}^2)^{1/2} = 0.16 \text{ m}$$

# Periodic Heating of Surface

If you solve heat conduction equation for the case where  
 $F = F_0 \cos(\omega t)$  is net heat flux through surface

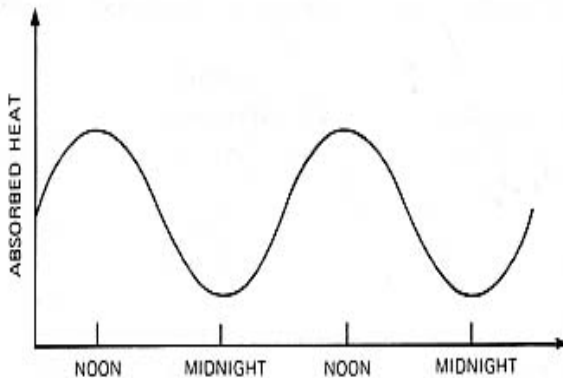
where  $\omega = \frac{2\pi}{\text{Period}} = \text{Angular frequency}$

$T = \frac{F_0}{P\sqrt{\omega}} \cos(\omega t - \frac{\pi}{4}) + T_0$  will be surface temperature.

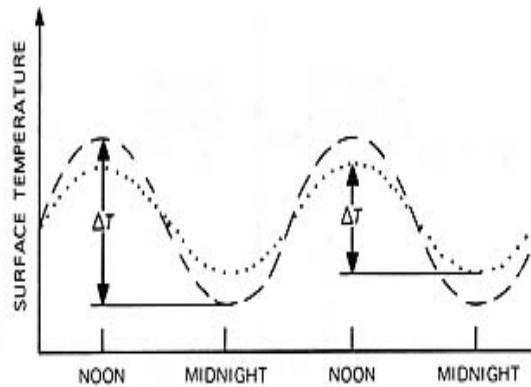
where  $P = \sqrt{K\rho C} = \text{Thermal Inertia}$  (most people use symbol  $\gamma$ , not P)

So amplitude of T variation is  $\propto F_0 / (P\omega^{1/2})$

Large thermal inertia  $\Rightarrow$  small T variation



A. Solar heating cycle.



--- MATERIALS WITH LOWER THERMAL INERTIA; SHALE, CINDERS. HIGH  $\Delta T$ .

..... MATERIALS WITH HIGHER THERMAL INERTIA; SANDSTONE, BASALT. LOW  $\Delta T$ .

B. Variations in surface temperature.

**Figure 5-6** Effect of differences in thermal inertia on surface temperatures during diurnal solar cycles. Note differences in  $\Delta T$  for materials with high and low thermal inertia.

Sabins Fig. 5-6

Note – figure is badly oversimplified.

T should really be delayed in phase

Also, NET flux is not sinusoidal.

# Basalt Thermal Inertia

For Basalt

$$P = \sqrt{K\rho C} = \sqrt{2.1 \text{ W m}^{-1} \text{ K}^{-1} \cdot 2800 \text{ kg m}^{-3} \cdot 840 \text{ J kg}^{-1} \text{ K}^{-1}}$$
$$= 2.2 \times 10^3 \text{ J m}^{-2} \text{ K}^{-1} \text{ s}^{-1/2}$$

If the net flux varied by  $500 \text{ W m}^{-2}$  (about  $1/3 F_{\text{sun}}$ )

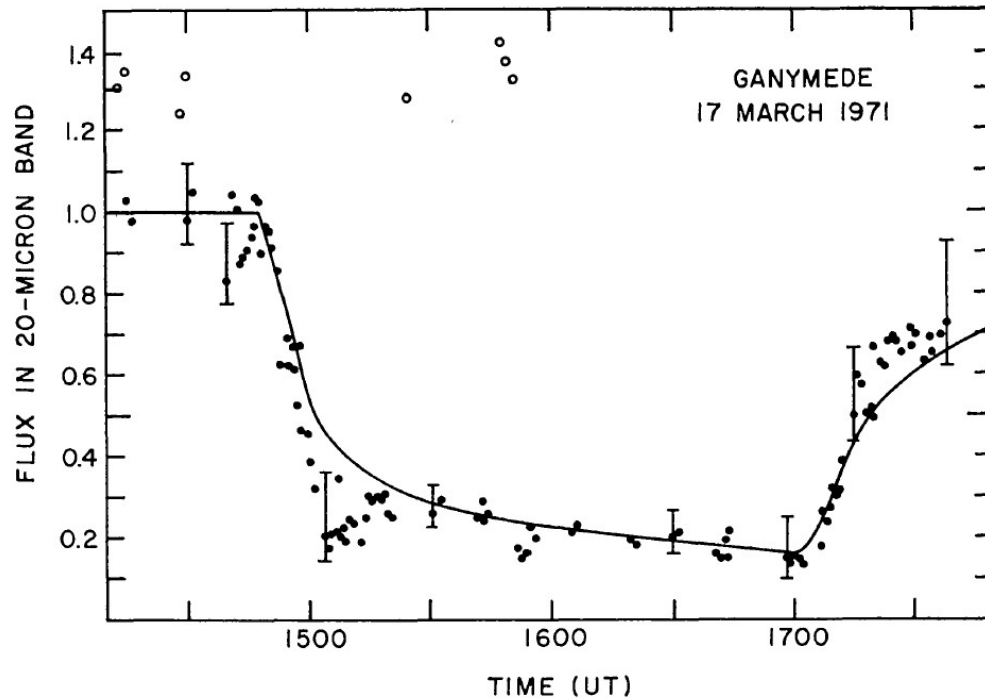
and the frequency  $\omega = \frac{2\pi}{1 \text{ day}} = \frac{2\pi}{8.64 \times 10^4 \text{ s}} = 7.27 \times 10^{-5} \text{ s}^{-1}$

then we would expect a temperature variation of

$$\frac{F_0}{P\sqrt{\omega}} = \frac{500 \text{ W m}^{-2}}{2.2 \times 10^3 \text{ J m}^{-2} \text{ K}^{-1} \text{ s}^{-1/2} \cdot \sqrt{7.27 \times 10^{-5} \text{ s}^{-1}}} = 26 \text{ K}$$

# Remote Determination of Thermal Inertia

- Despite what book says, you really can determine  $P$  remotely if you have  $(1-A) \times F_{\text{sun}}(t)$  and  $T(t)$ .



$$\begin{aligned}
 P &= 3 \times 10^4 \text{ erg cm}^{-2} \text{ s}^{-1/2} \text{ K}^{-1} \\
 &= 3 \times 10^{-3} \text{ J cm}^{-2} \text{ s}^{-1/2} \text{ K}^{-1} \\
 &= 7.2 \times 10^{-4} \text{ cal cm}^{-2} \text{ s}^{-1/2} \text{ K}^{-1}
 \end{aligned}$$

Text quotes sandy soil as  $0.050 (=5 \times 10^{-2}) \text{ cal cm}^{-2} \text{ s}^{-1/2} \text{ K}^{-1}$   
 so Ganymede resists  $T$  changes  $100 \times$  worse.

$P = (K \rho C)^{1/2}$   
 If change is due to  $K$ ,  
 it is  $10000 \times$  smaller, due to pulverized regolith

FIG. 2.—Radiometry of Ganymede compared with predicted  $20\text{-}\mu$  fluxes. *Filled circles*, measurements of Ganymede with sample estimated error bars indicated. *Open circles*, observations of Callisto (J IV). *Solid curve*, the prediction of the best-fitting homogeneous model, for which the thermal inertia is  $3 \times 10^4 \text{ ergs cm}^{-2} \text{ s}^{-1/2} \text{ K}^{-1}$ .

# Summary: Material Terms

$K$  Thermal conductivity  
How well material conducts heat

$C$  Heat capacity  
How much energy is stored

$\rho$  Mass per unit volume

$A$  Albedo  
Fraction of sunlight reflected

$\kappa = k = \frac{K}{\rho C}$  Thermal diffusivity  
How fast thermal wave travels

$\gamma = P = \sqrt{K\rho C}$  Thermal Inertial  
How well surface resists T changes

$ATI = \frac{1-A}{\Delta T}$  Apparent Thermal Inertia  
Simple observational measure of thermal inertia

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Simple observational measure of thermal inertia



# Typical Thermal Properties

Thermal diffusivity : Distance of propagation of thermal wave in time  $\Delta t$ ?

$$\Delta x = \sqrt{\frac{K}{\rho C} \Delta t}$$

For sandy soil and  $t = 1 \text{ day} = 8.6 \times 10^4 \text{ s}$

$$\Delta x = (3 \times 10^{-7} \text{ m}^2 \text{ s}^{-1} \times 8.6 \times 10^4 \text{ s})^{1/2} = (2.6 \times 10^{-2} \text{ m}^2)^{1/2} = 0.16 \text{ m}$$

Thermal inertia : Degree of resistance to temperature change

For Basalt

$$P = \sqrt{K\rho C} = \sqrt{2.1 \text{ W m}^{-1}\text{K}^{-1} \cdot 2800 \text{ kg m}^{-3} \cdot 840 \text{ J kg}^{-1} \text{K}^{-1}} = 2.2 \times 10^3 \text{ J m}^{-2} \text{K}^{-1} \text{ s}^{-1/2}$$

$$\text{Amplitude of } T \text{ diurnal variation} \approx \frac{F_0}{P\sqrt{\omega}} = 26 \text{ K}$$

(so  $\Delta T = 52\text{K}$ , probably an overestimate if we include atmospheric cooling, etc.)

# Thermal Inertia and diurnal cycle

Sabins Fig. 5-7

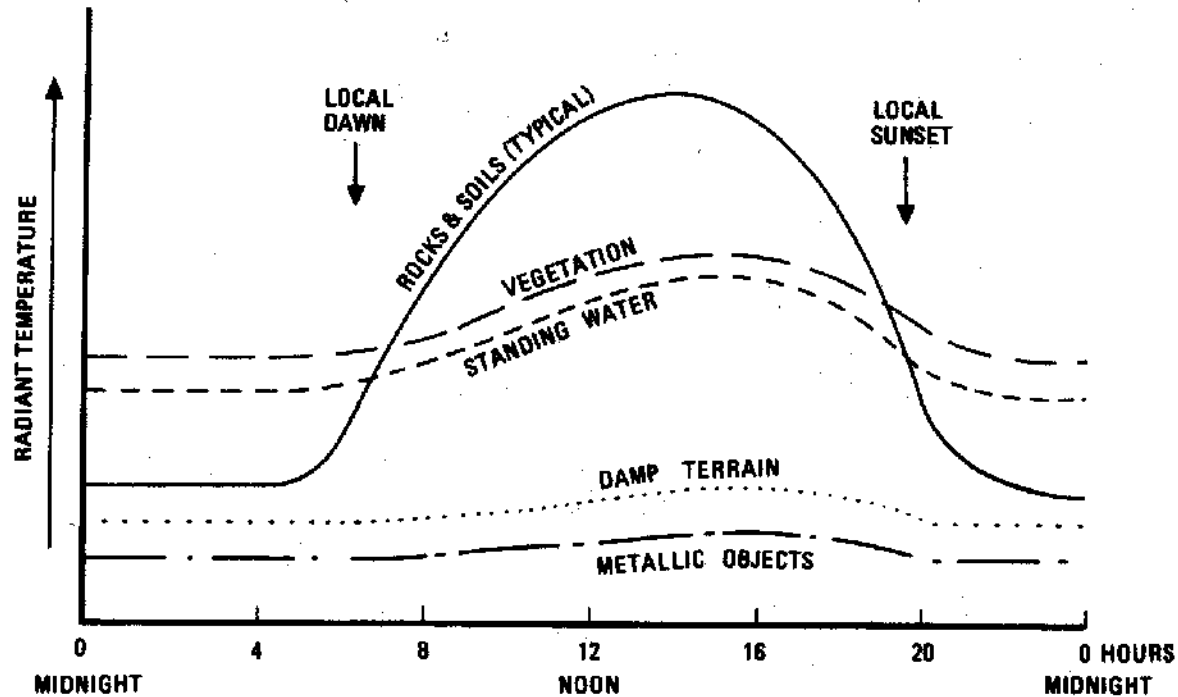


Figure 5-7 Diurnal radiant temperature curves (diagrammatic) for typical materials.

$$F_{\text{net}} = (1-A) F_{\text{sun}} - \sigma T^4$$

where  $A$  = Albedo

Wet soil has higher thermal conductivity so higher thermal inertia,

but it and vegetation are also affected by evaporation, which limits temperature rise.

# Crossover times for two materials

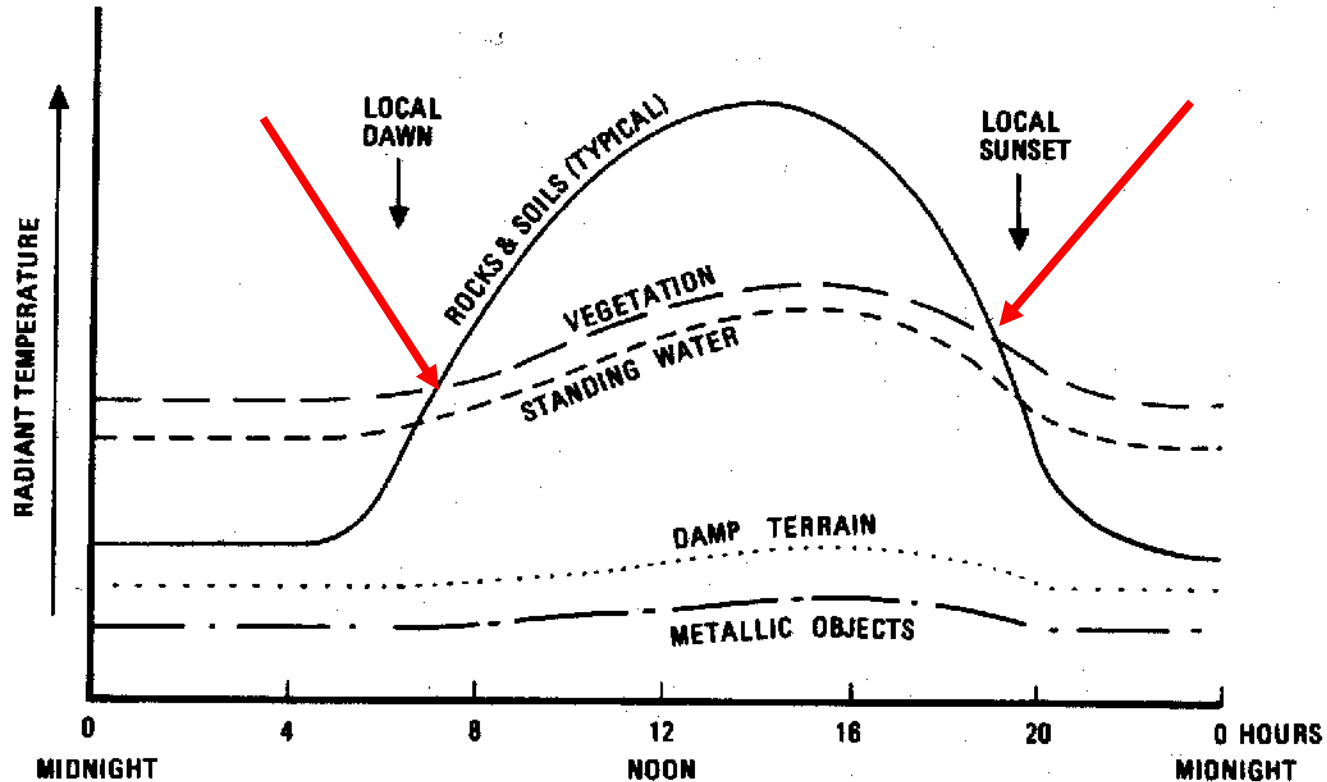
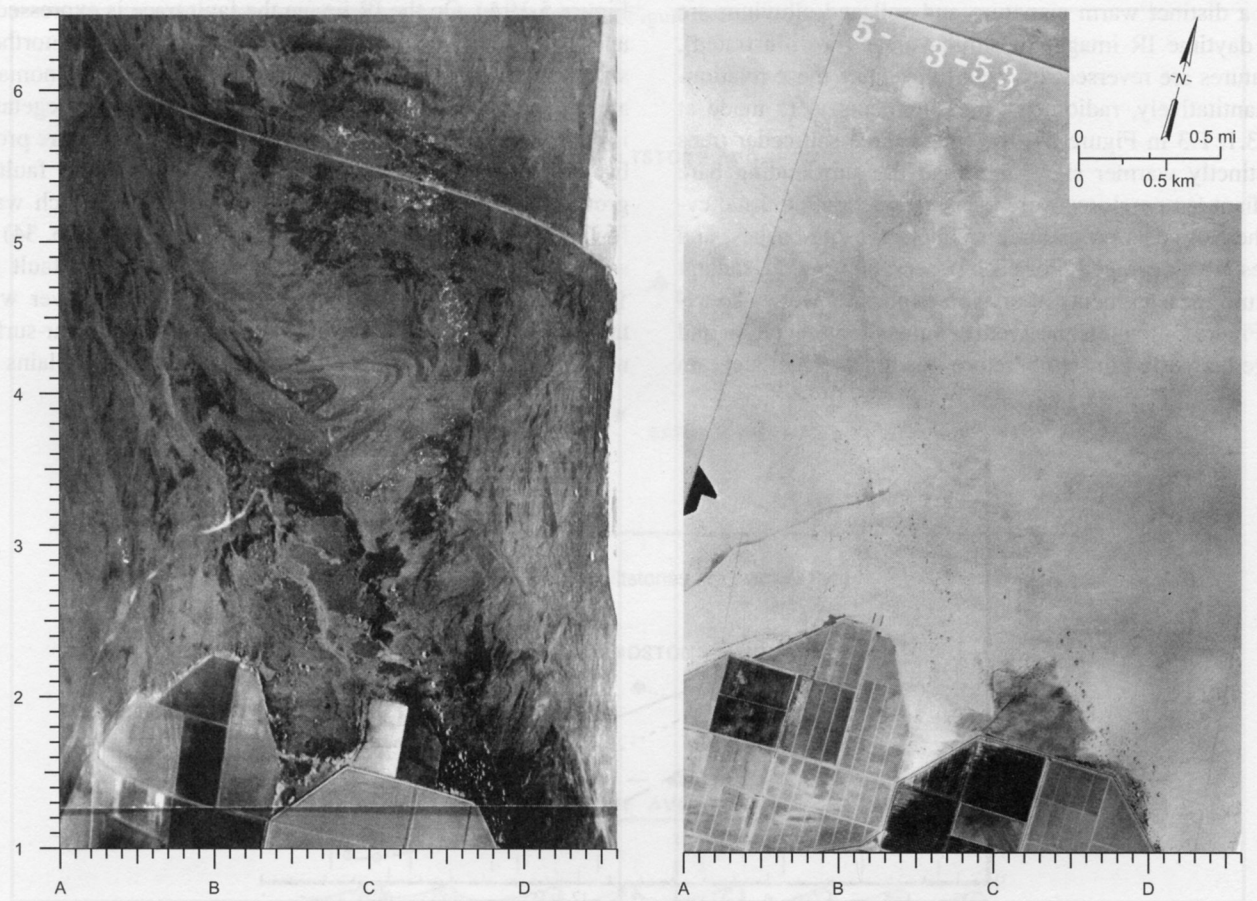


Figure 5-7 Diurnal radiant temperature curves (diagrammatic) for typical materials.

# Thermal Images: Imler Rd., CA



A. Nighttime thermal IR image (8 to 14  $\mu\text{m}$ ) acquired August 1961.

B. Aerial photograph acquired May 5, 1953.

**Figure 5-23** Images of the Imler Road area, Imperial County, California. From Sabins (1969, Plate 1).

How far does thermal wave propagate in given  $\Delta t$ ?

Assume given  $\Delta T$ , solve for  $\Delta x$ :

$$\Delta x = \sqrt{\frac{K}{\rho C} \Delta t}$$

=0.16 m in sandy soil in 24 hr.

Sabins Fig. 5-23 & 5-25 pg. 158-159 Aerial Photo, Nighttime IR, Imler Rd. CA  
Gravel and windblown sand conceal bedrock. Cover thinner than diurnal skin depth.

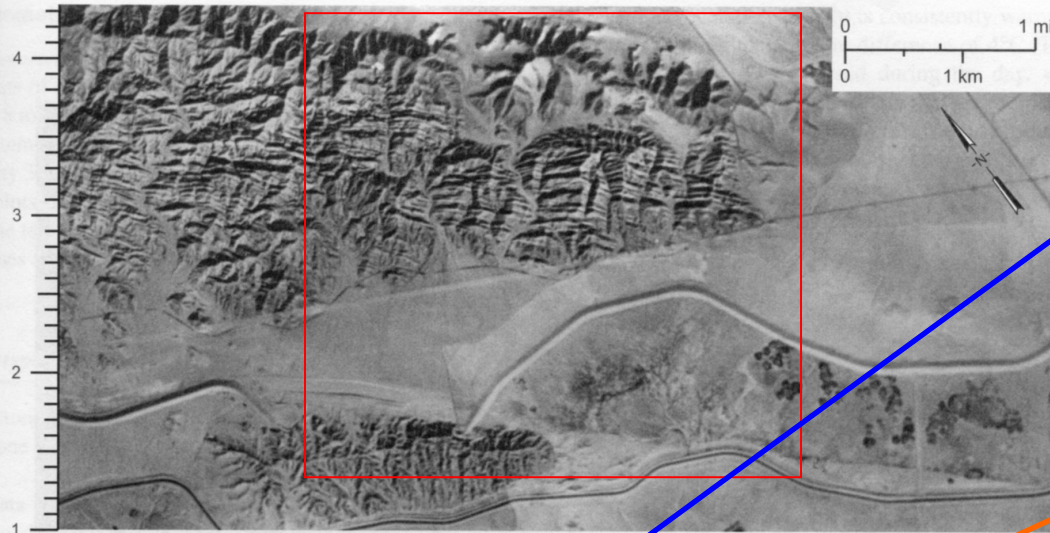
# Thermal Images: Imler Rd., CA



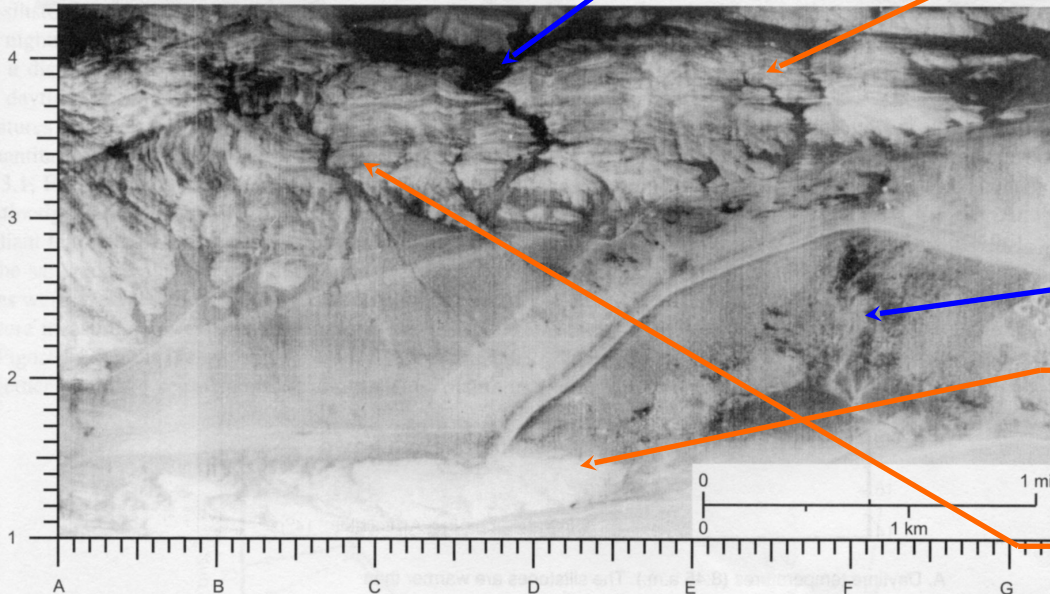
Sabins Fig. 5-23 & 5-25 pg. 158-159 Aerial Photo, Nighttime IR, Imler Rd. CA  
 Gravel and windblown sand conceal bedrock. Cover thinner than diurnal skin depth.

# Aerial Photo and Night Thermal Imagery, Indio Hills

Sabins Fig. 5-19 pg 155



A. Aerial photograph acquired May 5, 1953.



B. Nighttime thermal IR image (8 to 14  $\mu\text{m}$ ) acquired October 1963.

Cool:

Alluvium?

Damp?

Shadows?

Palm Springs Formation:  
alternating beds of resistant  
conglomerate sandstone and  
nonresistant siltstone

Alluvium

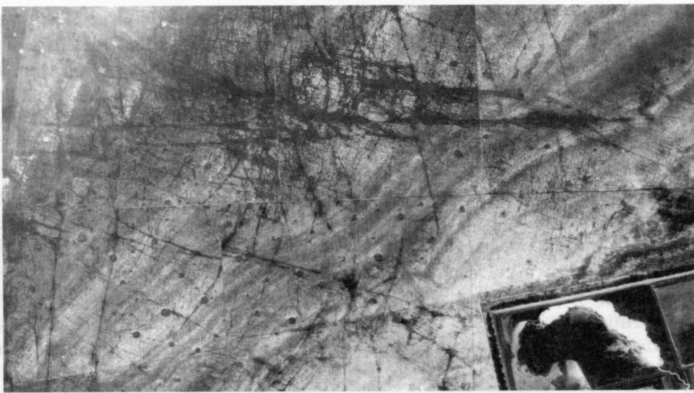
Vegetation

Ocotillo Conglomerate:  
Poorly stratified

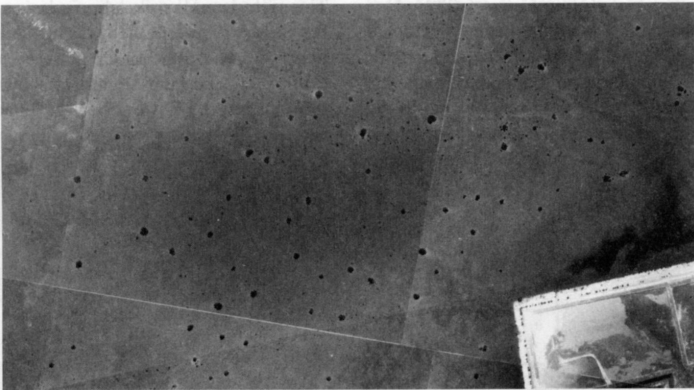
Syncline and Anticline

# Thermal Images: Stilfontein

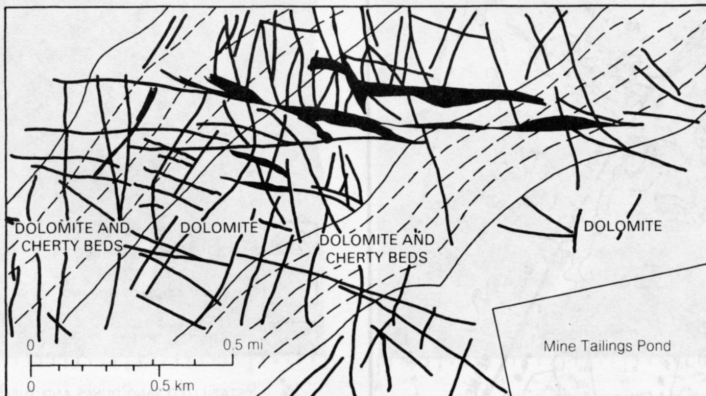
Sabins Fig. 5-25 pg. 160  
Aerial Photo, Nighttime IR, Interpretation  
Stilfontein, South Africa



A. Nighttime thermal IR image (8 to 14  $\mu\text{m}$ ).



B. Aerial photograph.



C. Interpretation map of thermal IR image.

**Figure 5-25** Stilfontein area, western Transvaal, South Africa. From Warwick, Hartopp, and Viljoen (1979, Figures 8 and 9).

Dark linear features: Faults and joints filled with moist soil

Dolomite: Warm (bright) High  $\rho$  and Thermal Inertia

Chert-Rich beds: Cool (dark) Low  $\rho$  and Thermal Inertia

# Apparent Thermal Inertia

- Simplified version is often used in terrestrial remote sensing:

- Apparent Thermal Inertia 
$$ATI = \frac{1 - A}{\Delta T}$$

$$\text{where } \Delta T = T_{\max} - T_{\min}$$

- Works because  $F_{\text{sun}}$  is roughly similar “everywhere” on Earth
- Can make an “ATI” image from a visible image (to get A) and a day and a night thermal image (to get  $T_{\max}$  and  $T_{\min}$ ).



# ATI Derivation for San Rafael Swell, Utah

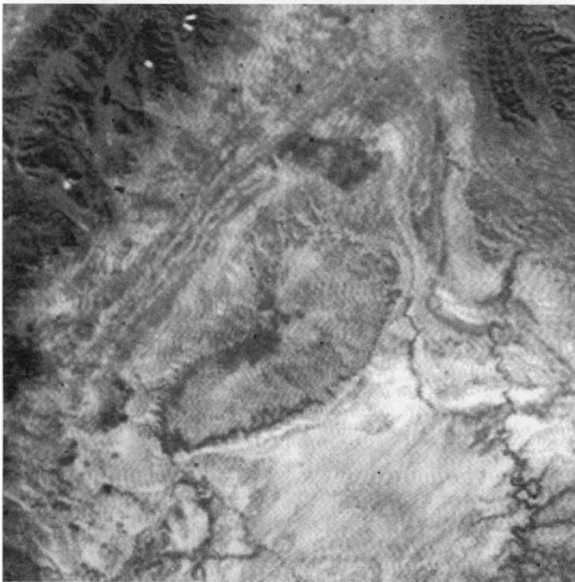
$$ATI = \frac{1 - A}{\Delta T}$$



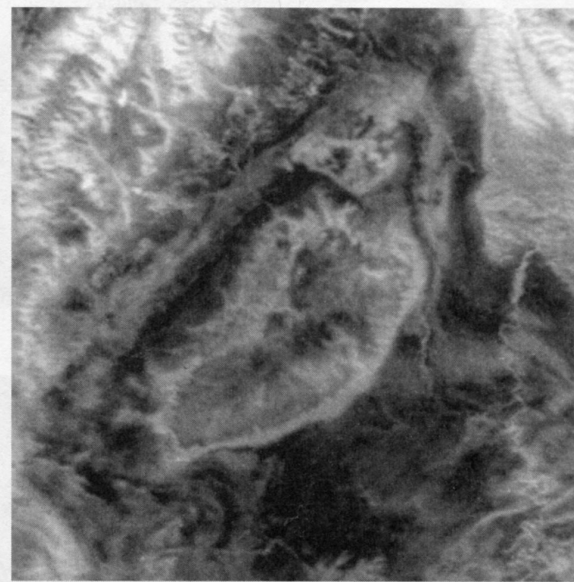
A. Daytime thermal IR image (10.5 to 12.5  $\mu\text{m}$ ) acquired August 28, 1978.



B. Nighttime thermal IR image (10.5 to 12.5  $\mu\text{m}$ ) acquired August 27, 1978.



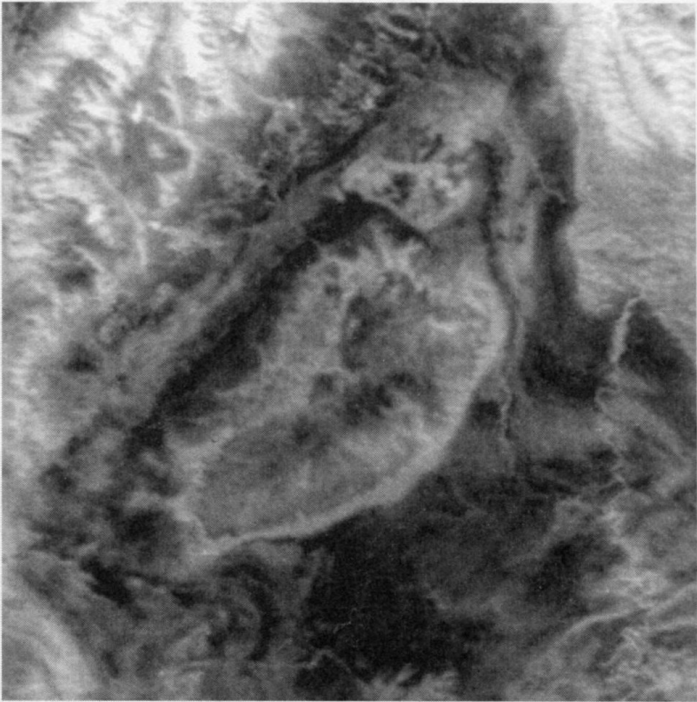
C. Visible (albedo) image acquired August 28, 1978.



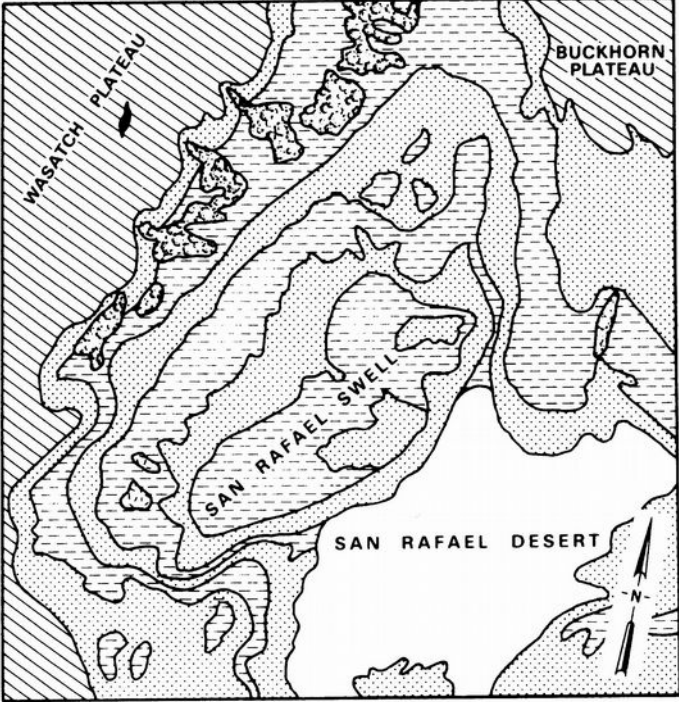
D. Apparent thermal inertia image.

**Figure 5-33** Enlarged HCMM images of the San Rafael Swell, Utah. From Kahle and others (1981).  
Courtesy A. B. Kahle, Jet Propulsion Laboratory.

# ATI Interpretation, San Rafael Swell, Utah



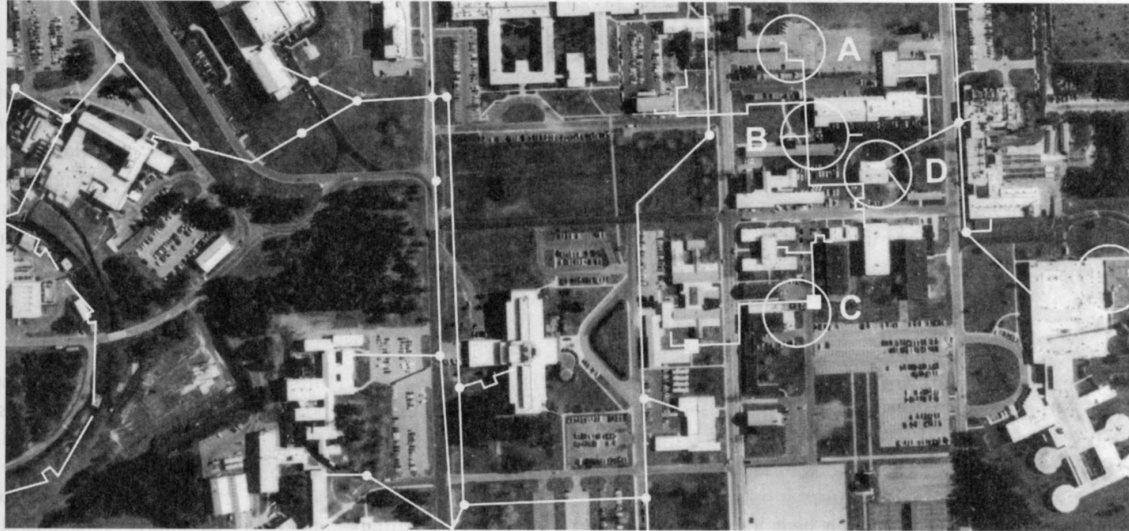
D. Apparent thermal inertia image.



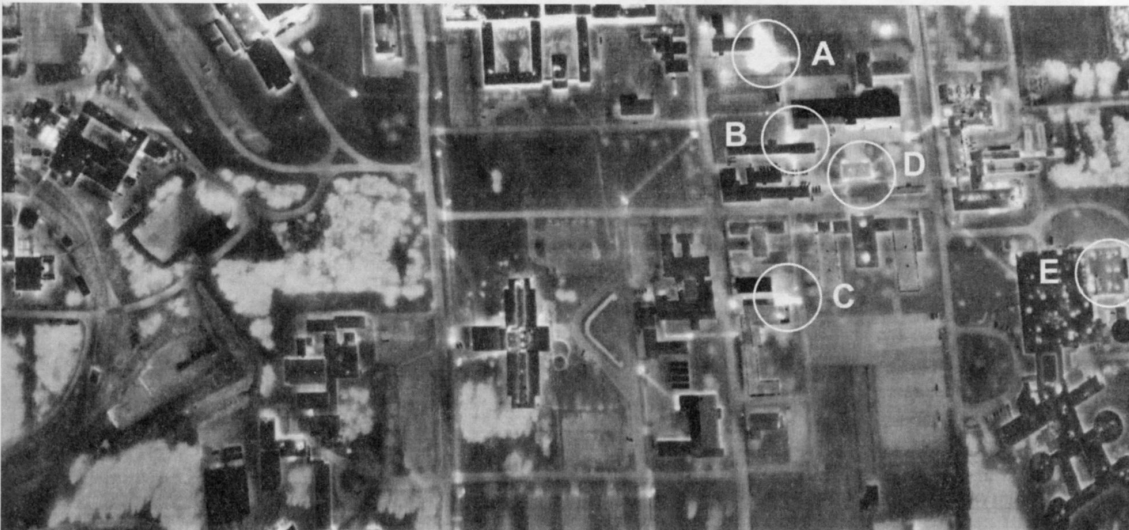
APPARENT THERMAL INERTIA	MAP SYMBOL	TERRAIN FEATURE
High and Intermediate		Plateau Terrain
High		Water
Intermediate		Vegetation
Intermediate		Sandstone
Intermediate		Igneous Rocks
Low		Shale
Low		Windblown Sand

Sabins Fig. 5-33d and 5-34

# Urban Heat Loss



A. Aerial photograph with overlay of heating lines.

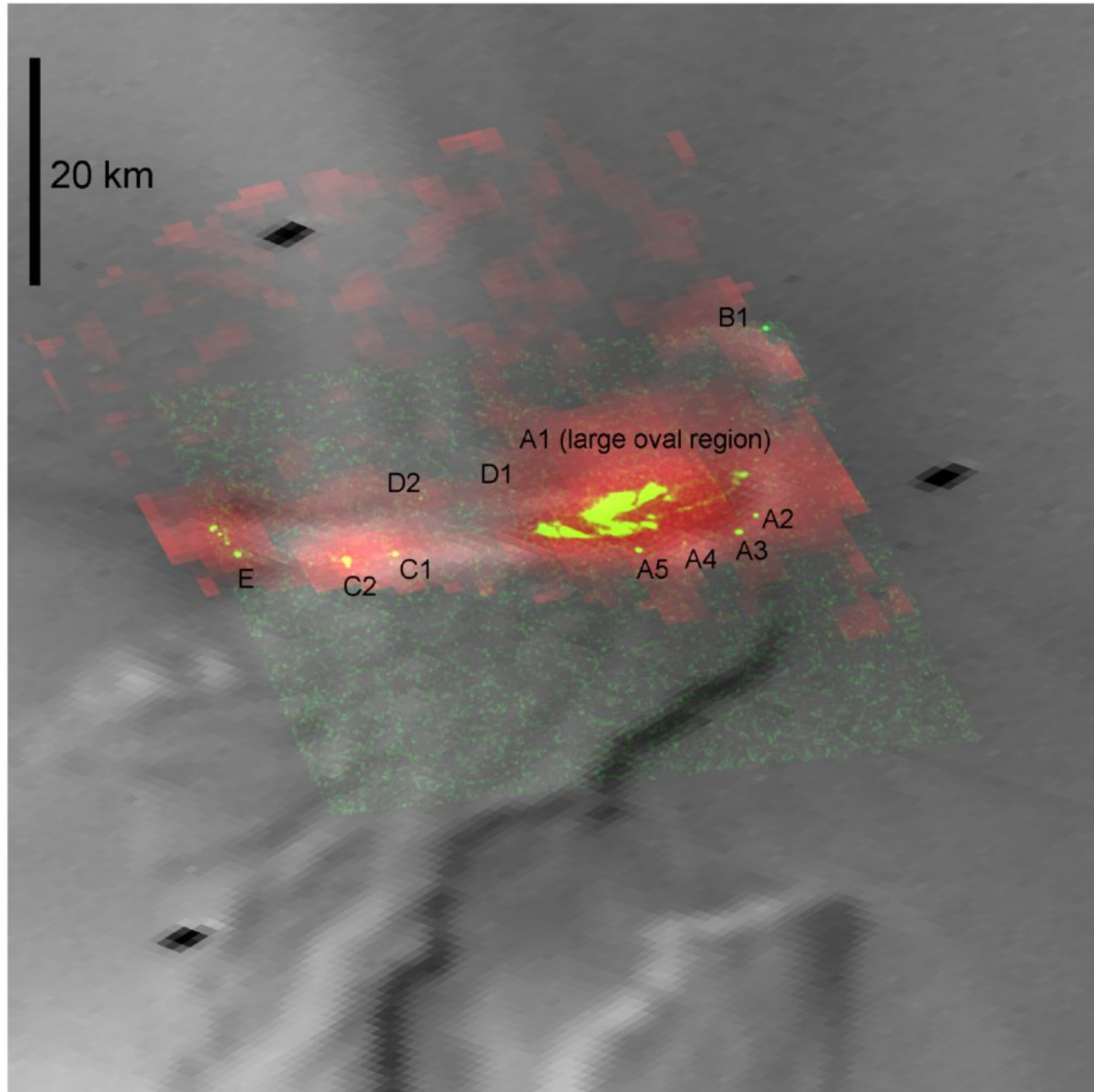


B. Night thermal IR image (8 to 14  $\mu\text{m}$ ).

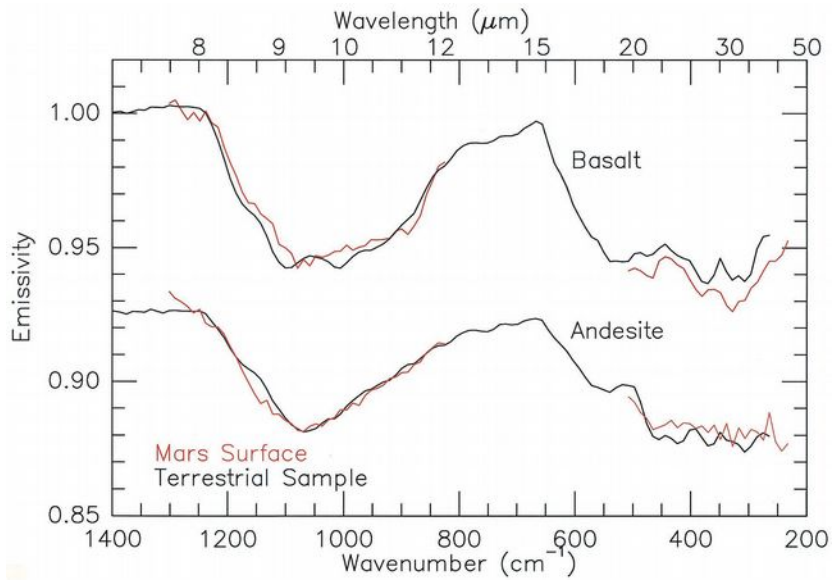
**Figure 5-17** Heat-loss survey of Brookhaven National Laboratories, Long Island, New York. Localities are explained in the text. Courtesy Daedalus Enterprises, Inc.

Sabins Fig. 5-17

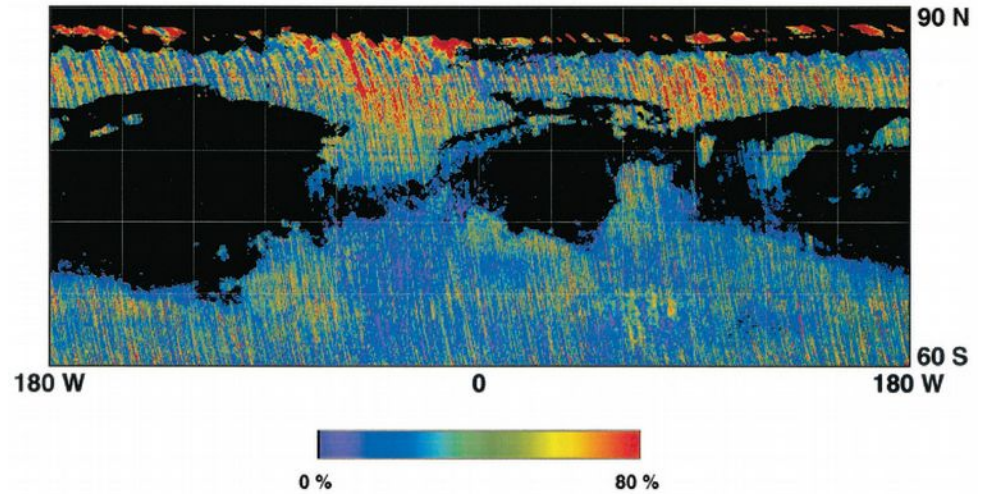
# Io Volcanism: Pele



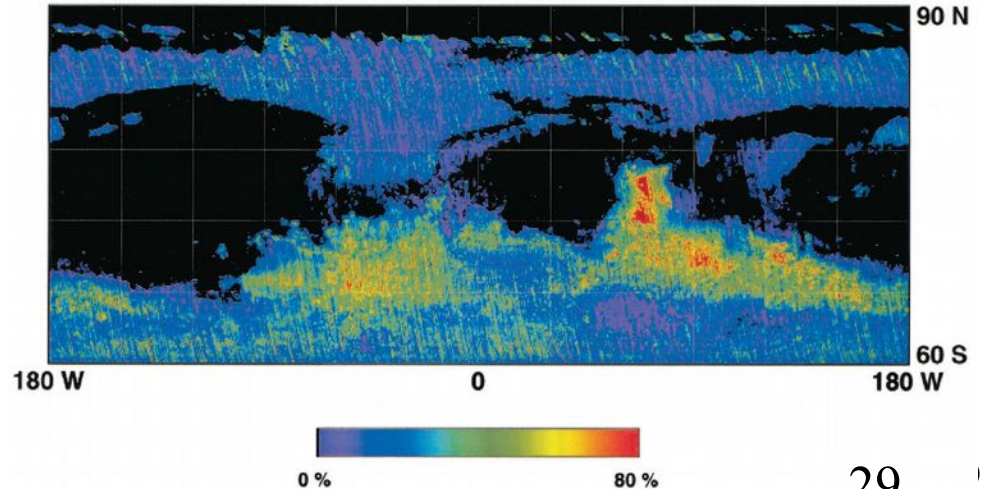
# Mars "TES" Results



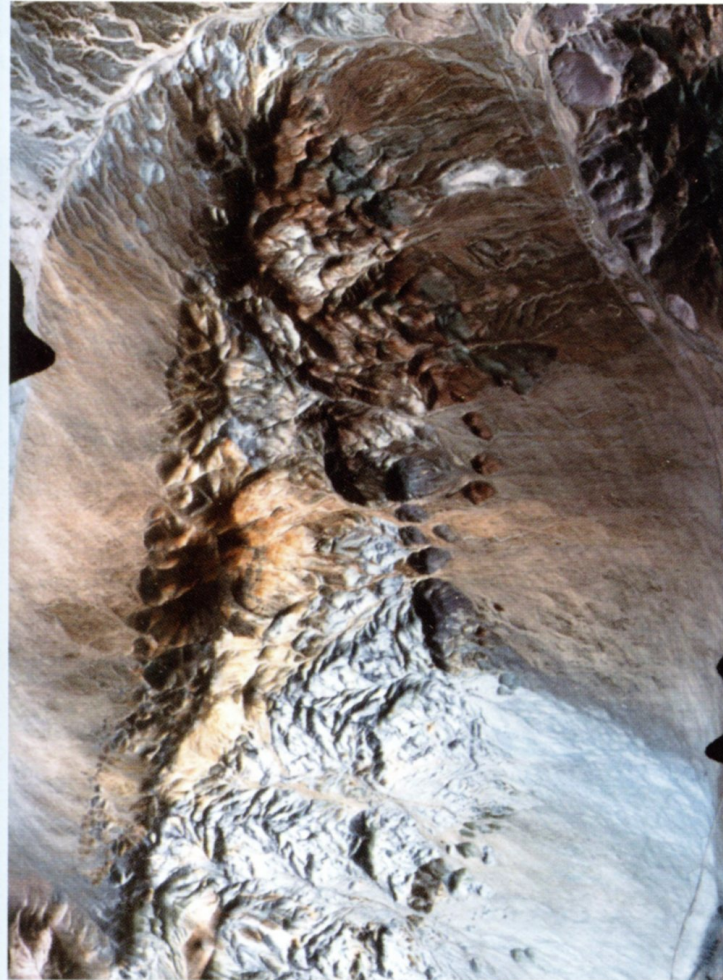
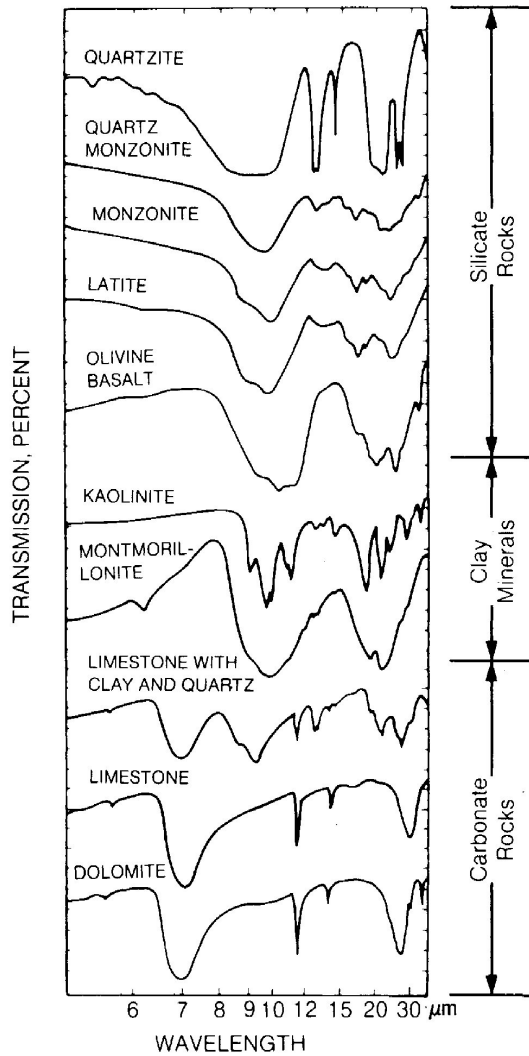
## TES Andesite Abundance



## TES Basalt Abundance



# TIMS: Cuprite Hills, NV

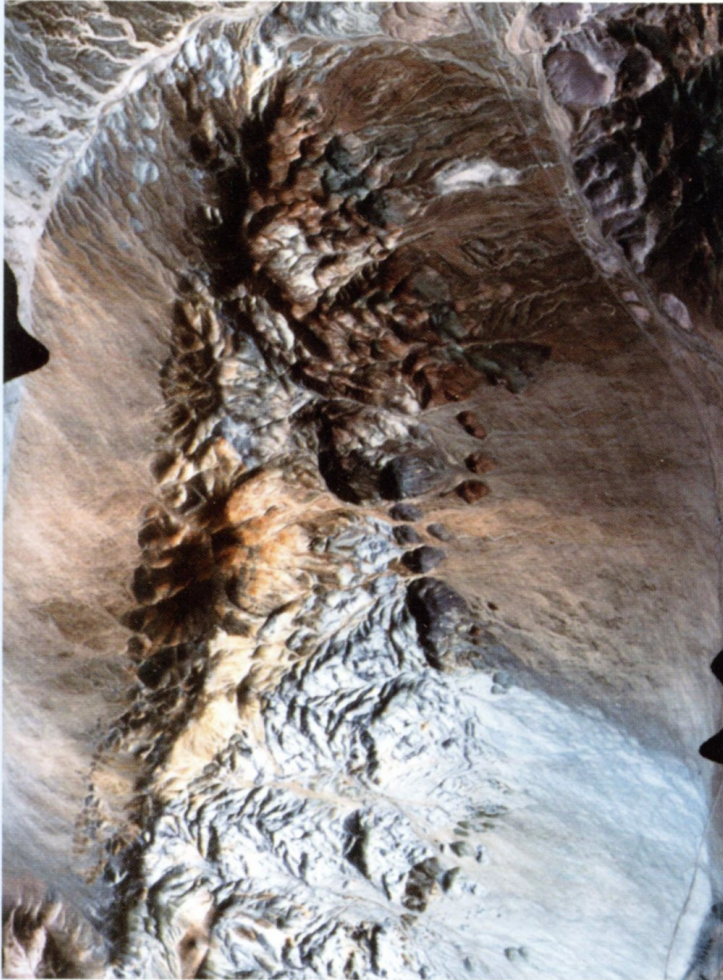


B. TIMS image showing kinetic temperature and emissivity, Cuprite Hills, Nevada.

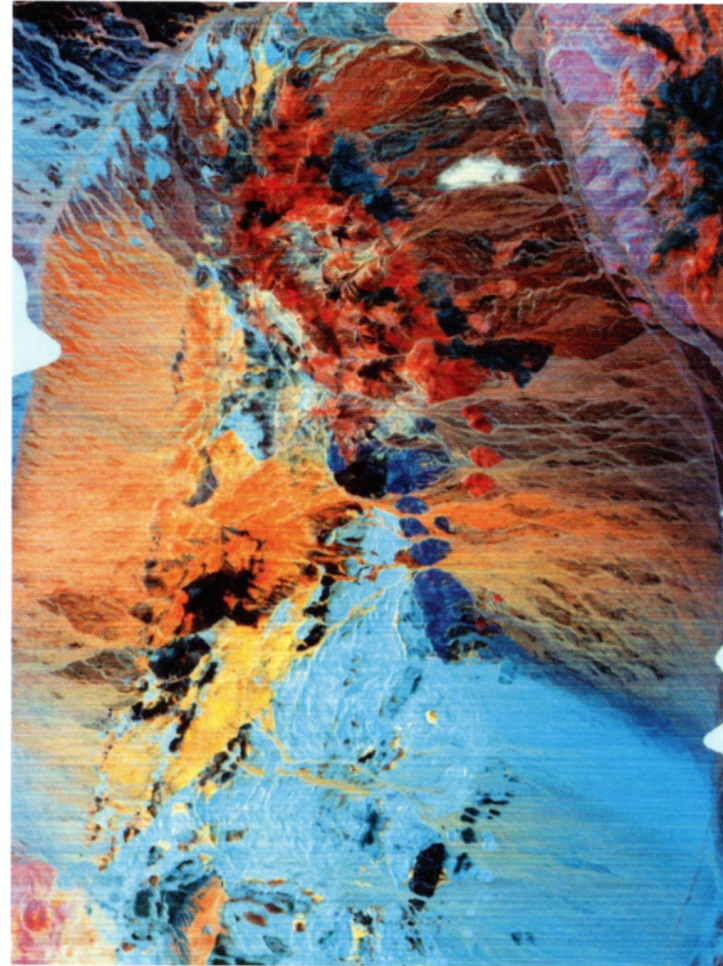
Sabins: TIMS image showing bands 3,2,1 as RGB

Figure 5-37 Thermal IR spectra of rocks and minerals. Spectra are offset vertically. From Kahle (1984, Figure 4).

# TIMS: Cuprite Hills, NV



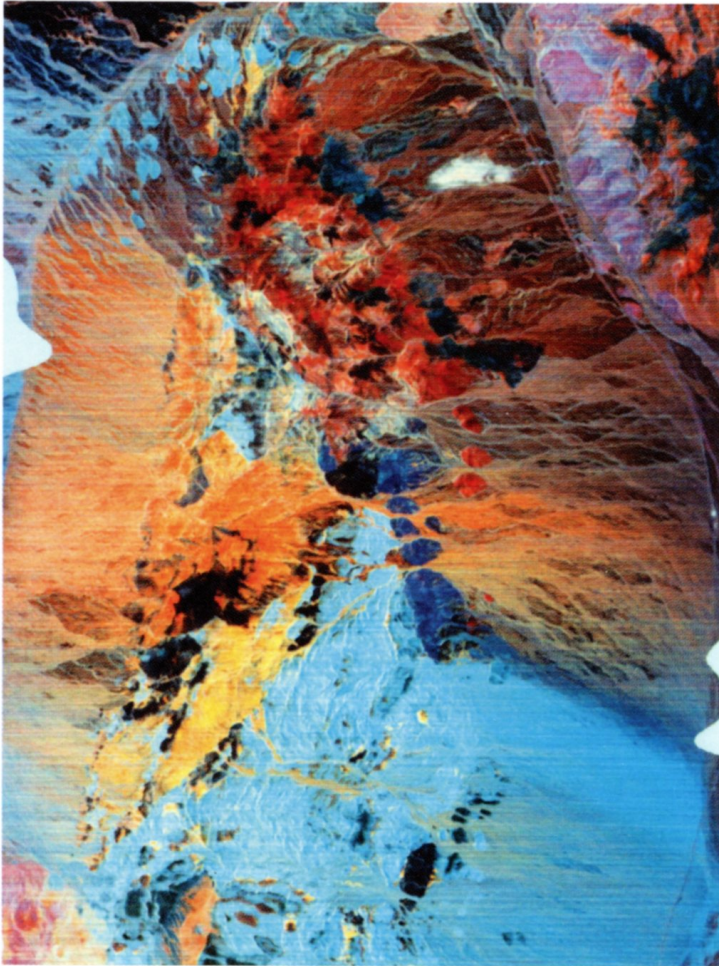
B. TIMS image showing kinetic temperature and emissivity, Cuprite Hills, Nevada.



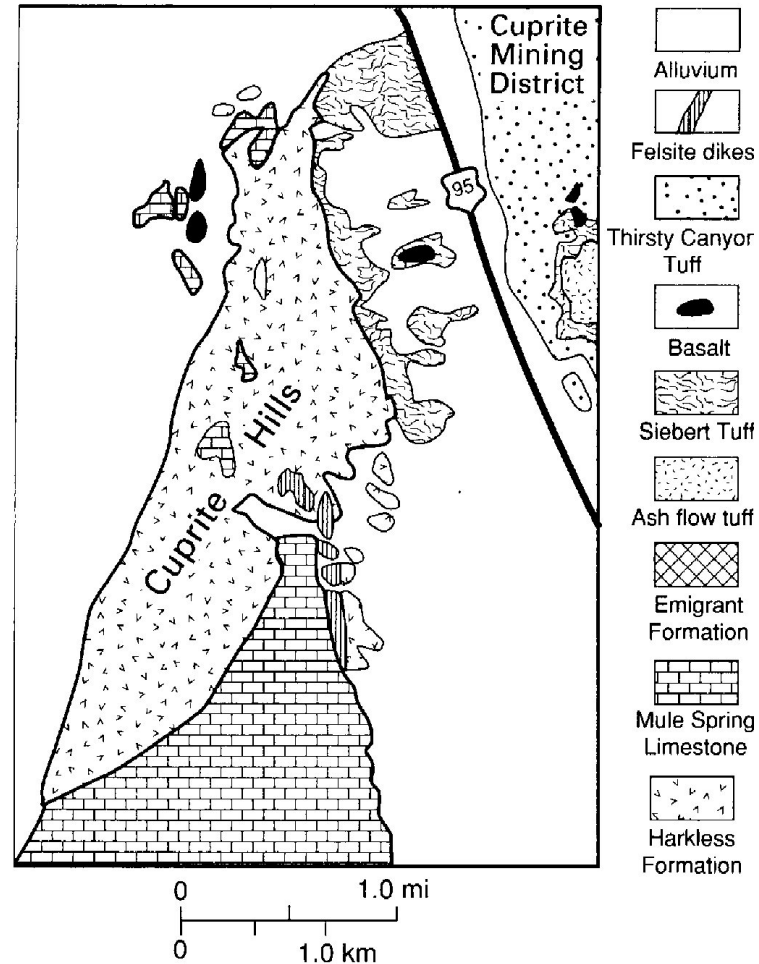
C. TIMS image showing emissivity information, Cuprite Hills, Nevada.

Sabins: TIMS image showing bands 3,2,1 as RGB, then image showing emissivity variations

# TIMS: Cuprite Hills, NV



C. TIMS image showing emissivity information, Cuprite Hills, Nevada.



**Figure 5-38** Interpretation map of TIMS images of the Cuprite Hills, Nevada. From Hook and others (1992, Figure 5).