

Mon. Feb. 26, 2018

- Midterm exam date:
  - Mon. Mar. 5 or Wed. Mar 7 (decide today in class)
- Reading: Sabins Ch. 5 (Thermal)
- Finish:
  - Theory of mineral absorptions (not in text)
    - Use slides posted for last Monday
- Thermal Remote Sensing

Use previously posted slides for  
Absorption Theory

# Thermal Radiation Intro.

- Thermal Emission – Application (mostly Monday)
  - Direct measurements of temperature (volcanoes, weather, etc.)
  - Mineral composition through “emissivity” (how well it radiates thermal IR)
  - Indirect information from heating & cooling rates (thermal inertia)
- Thermal Emission – Theory
  - Planck Blackbody formula
  - Stefan-Boltzmann law and Wien displacement law
  - Kilauea Aster examples
  - Emissivity
    - Emissivity spectra of silicates and other minerals
    - Emissivity mapping of Mars
  - Thermal Inertia (Monday.)

# Temperature and Heat

- Thermal energy is “kinetic energy” of moving atoms and molecules
- Want temperature scale where energy is proportional to T
  - Celsius scale is “arbitrary” (Fahrenheit even more so)
    - $0^{\circ}\text{C}$  = freezing point of water
    - $100^{\circ}\text{C}$  = boiling point of water
  - By experiment, available energy = 0 at “Absolute Zero” =  $-273^{\circ}\text{C}$  ( $-459.7^{\circ}\text{F}$ )
  - Define “Kelvin” scale with same step size as Celsius, but  $0\text{K} = -273^{\circ}\text{C} = \text{Absolute Zero}$
- Use Kelvin Scale for most of work in this course
  - Available energy is proportional to T, making equations simple
  - $273\text{K}$  = freezing point of water
  - $373\text{K}$  = boiling point of water
  - $300\text{K}$  approximately room temperature

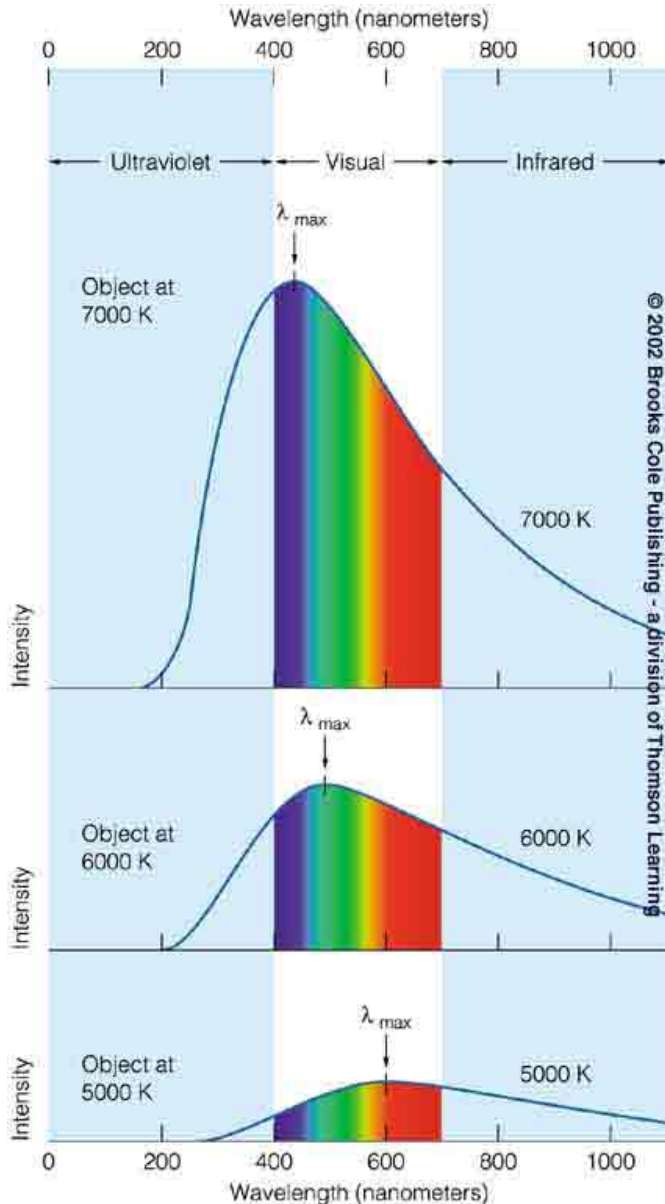
# Thermal Energy Transfer

- Conduction
  - molecule – to – molecule (contact)
- Convection
  - motion of material carrying heat
- Radiation
  - electromagnetic radiation

# Planck “Black Body Radiation”

- Hot objects glow (emit light)
- Reason for name “Black Body Radiation”
  - A material which reflects light also has trouble emitting it:
    - reflectance + absorbance + transmission = 1
    - reflectance + absorbance = 1 if transmission negligible
  - A black material in one which readily absorbed all wavelengths of light. These turn out to be the same materials which also readily emit all wavelengths when hot.
    - reflectance + emissivity + transmission = 1
    - reflectance + emissivity = 1 if transmission negligible
    - $r + \varepsilon = 1$  (at given  $\lambda$ )
    - In thermal infrared, most materials are opaque so this rule holds (and usually  $r \ll 1$ ,  $\varepsilon \cong 1$ )
- The hotter the material the more energy it emits as light
  - As you heat up a filament or branding iron, it glows brighter and brighter
- The hotter the material the more readily it emits high energy (blue) photons
  - As you heat up a filament or branding iron, it first glows dull red, then bright red, then orange, then if you continue, yellow, and eventually blue

# Planck and other Formulae



- **Planck formula** gives intensity of light at each wavelength

$$B(\lambda, T) = \frac{C_1 \lambda^{-5}}{e^{C_2/(\lambda T)} - 1}$$

- It is complicated. Often we'll use two simpler formulae which can be derived from it.
- **Wien's law** tells us what wavelength has maximum intensity

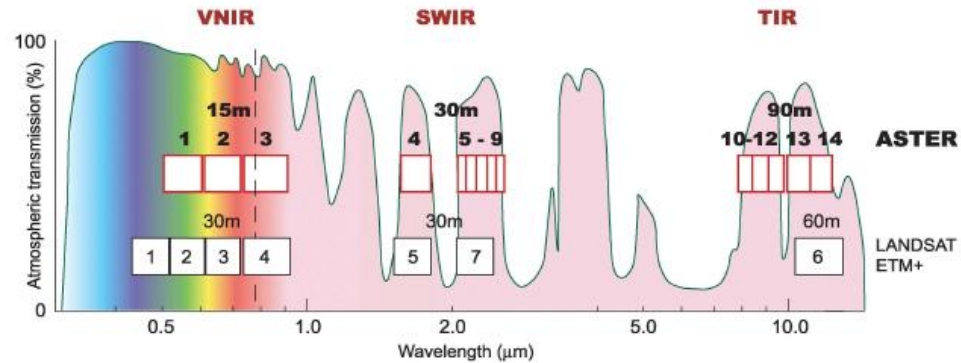
$$\lambda_{\text{Max}} = \frac{3,000,000 \text{ nm K}}{T} = \frac{3,000 \mu\text{m K}}{T}$$

- **Stefan-Boltzmann law** tells us total radiated energy per unit area

$$F = \sigma T^4 \text{ where } \sigma = 5.67 \times 10^{-8} \text{ W}/(\text{m}^2 \text{ K}^4)$$

From Horizons, by Seeds

# TM and Aster Thermal Channels



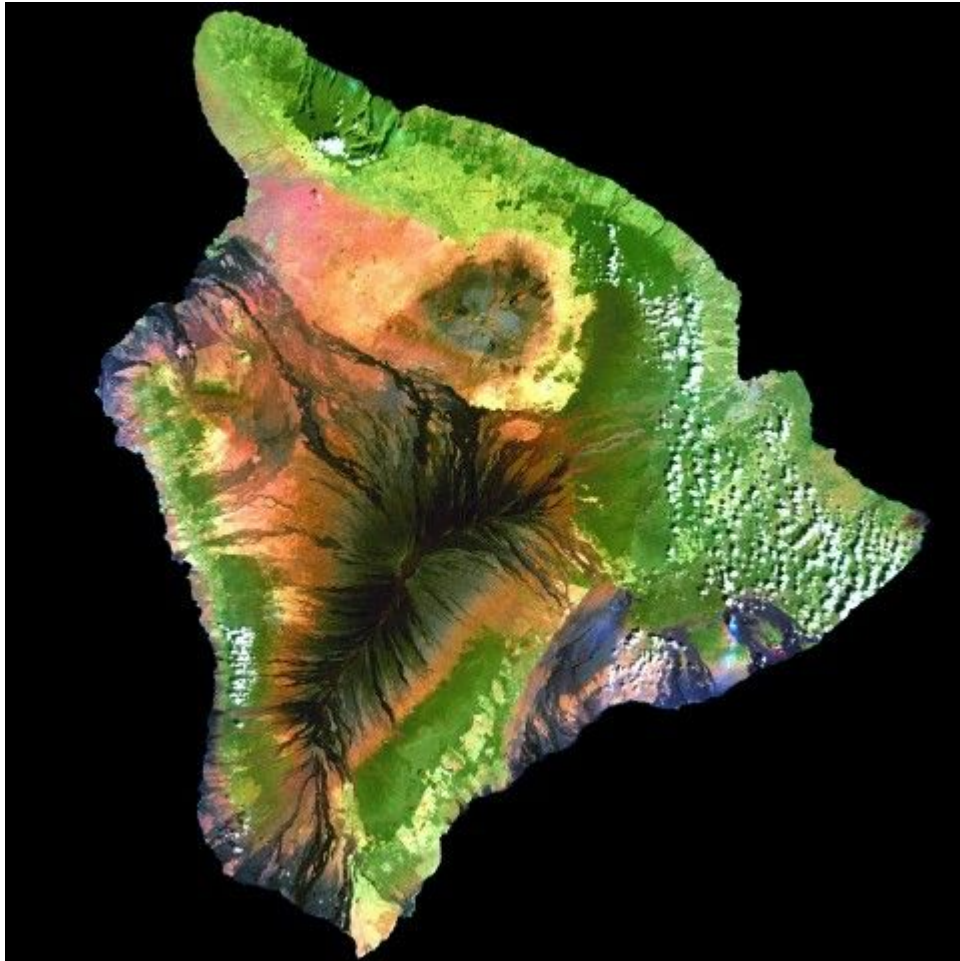
Landsat TM has Band 6 at  $\sim 10 \mu\text{m}$   
120 m resolution on TM

60 m resolution on ETM+ (Landsat 7)

Aster has bands 10-14, 90 m resolution



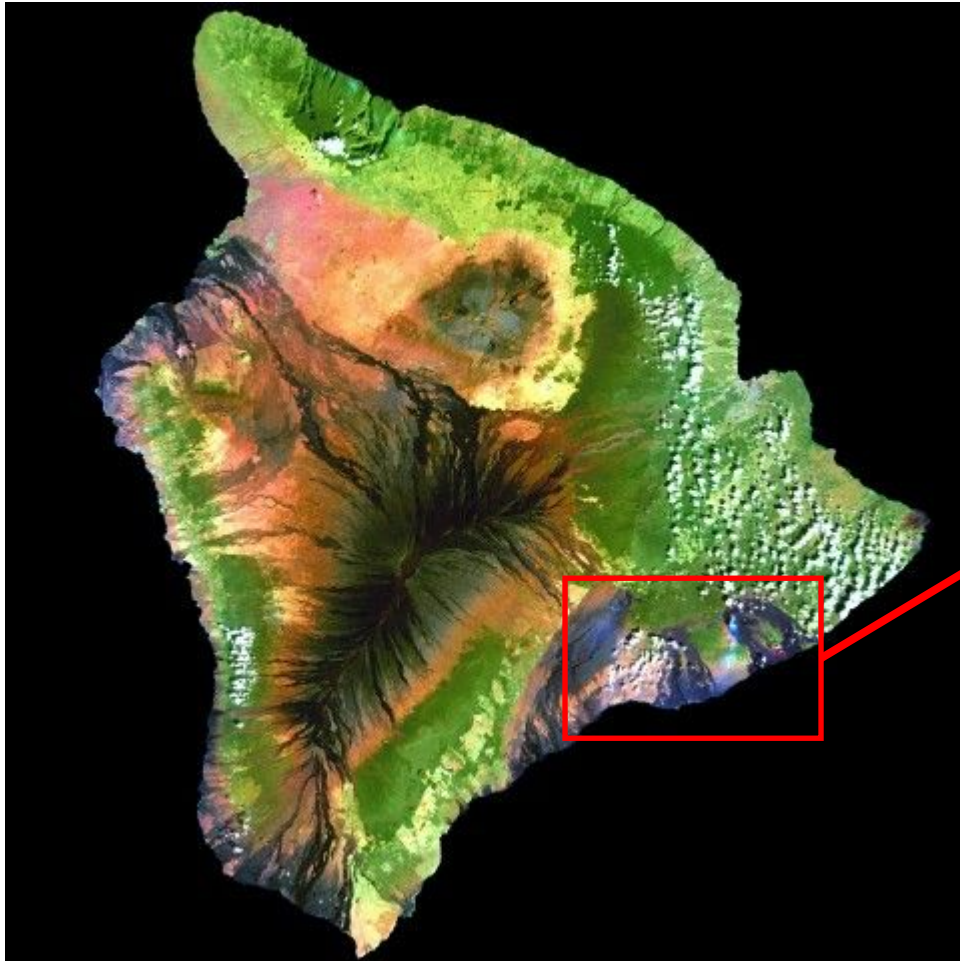
# Big Island of Hawaii



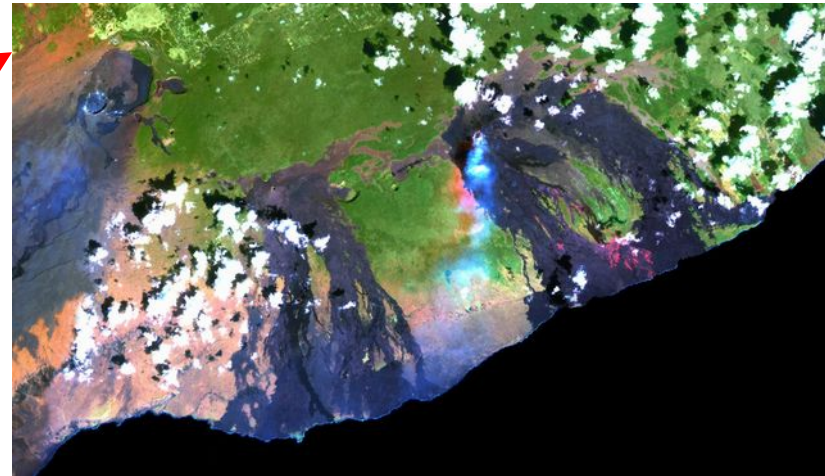
Hot objects glow (emit light)

Landsat Mosaic

# Big Island of Hawaii

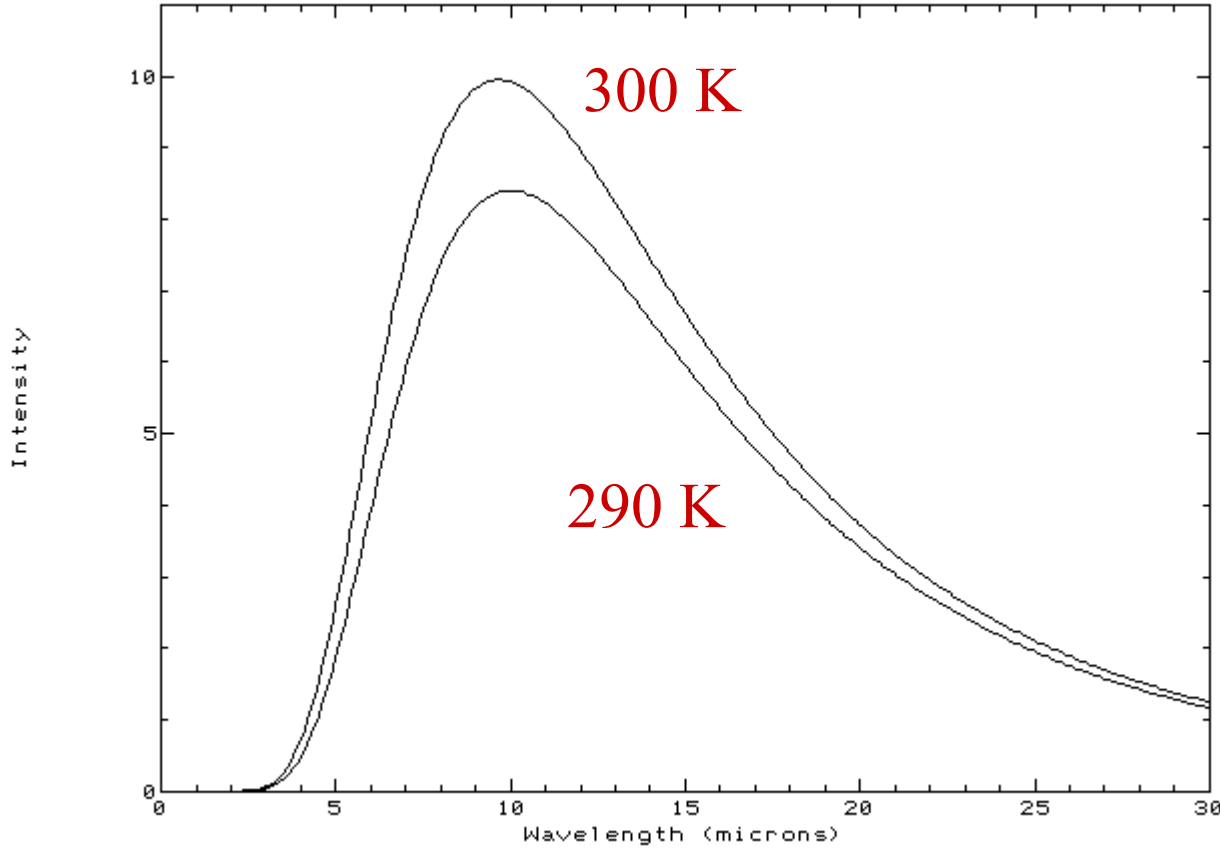


Kilauea



Landsat Mosaic

# Planck Blackbody Curves

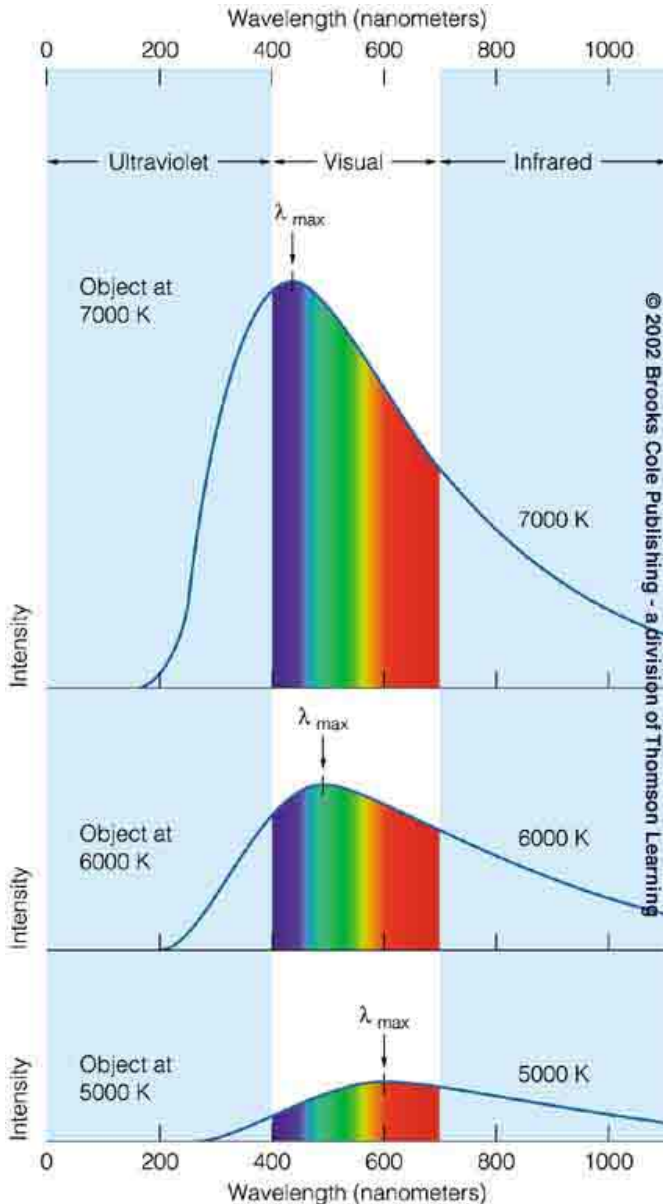


$$B(\lambda, T) = \frac{C_1 \lambda^{-5}}{e^{\frac{C_2}{\lambda T}} - 1}$$

Units of I (or B)

Watts  $\text{m}^{-2} \mu\text{m}^{-1} \text{str}^{-1}$

# Color Temperature vs. Brightness Temperature



- If you measure intensity at many wavelengths, find  $\lambda$  where  $I$  is maximum (i.e. intensity  $\lambda_{\max}$ ) then use Wien's law to solve for  $T$

$$\lambda_{\text{Max}} = \frac{3,000 \mu\text{m K}}{T} \quad \frac{3,000 \mu\text{m K}}{\lambda_{\text{Max}}}$$

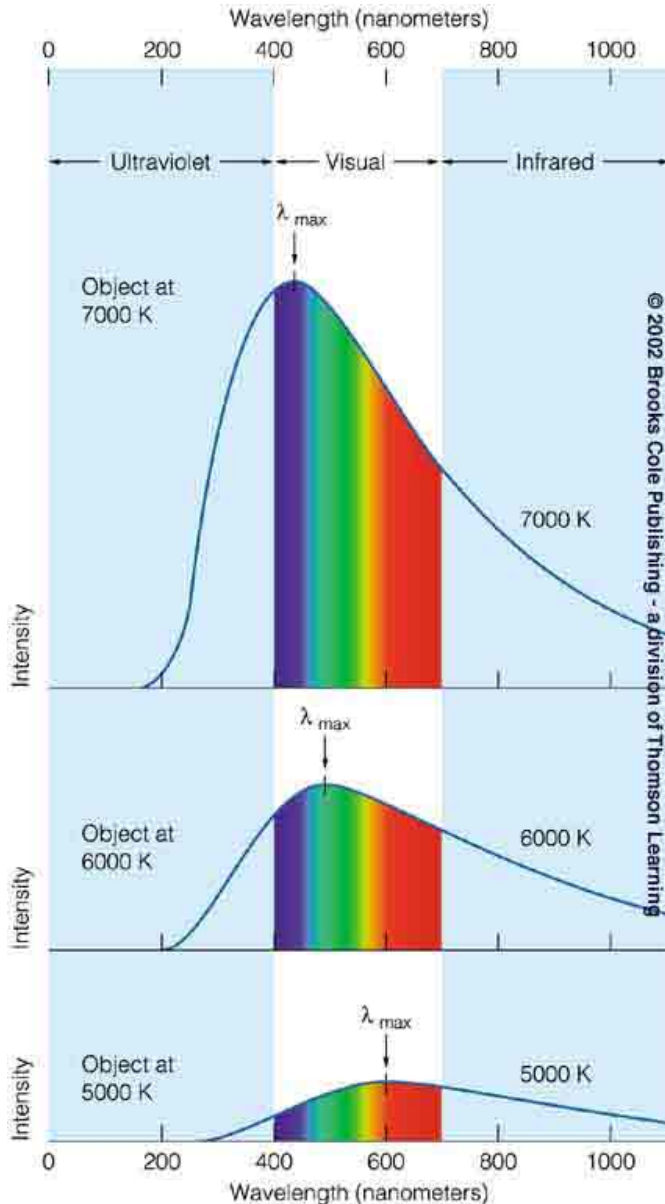
- Examples – Room  $T$ , Volcanic  $T$

$$T = \frac{3,000 \mu\text{m K}}{10 \mu\text{m}} = 300 \text{ K} \quad T = \frac{3,000 \mu\text{m K}}{3 \mu\text{m}} = 1000 \text{ K}$$

- Advantage of color  $T$ : Don't need to know area of source.
- Even if you just know  $I$  at two  $\lambda$  you can find color  $T$  because ratio  $I_1/I_2 = B(\lambda_1, T)/B(\lambda_2, T)$  doesn't depend on area  
Can solve (complicated equation) for  $T$

$$B(\lambda, T) = \frac{C_1 \lambda^{-5}}{e^{C_2/(\lambda T)} - 1}$$

# Color Temperature vs. Brightness Temperature



- If you know area of source so you have measured I or F then you can solve for Brightness Temperature using either Stefan-Boltzmann equation or Planck's Equation

$$F = \sigma T^4 \text{ where } \sigma = 5.67 \times 10^{-8} \text{ W}/(\text{m}^2 \text{ K}^4)$$

$$T = (F/\sigma)^{1/4}$$

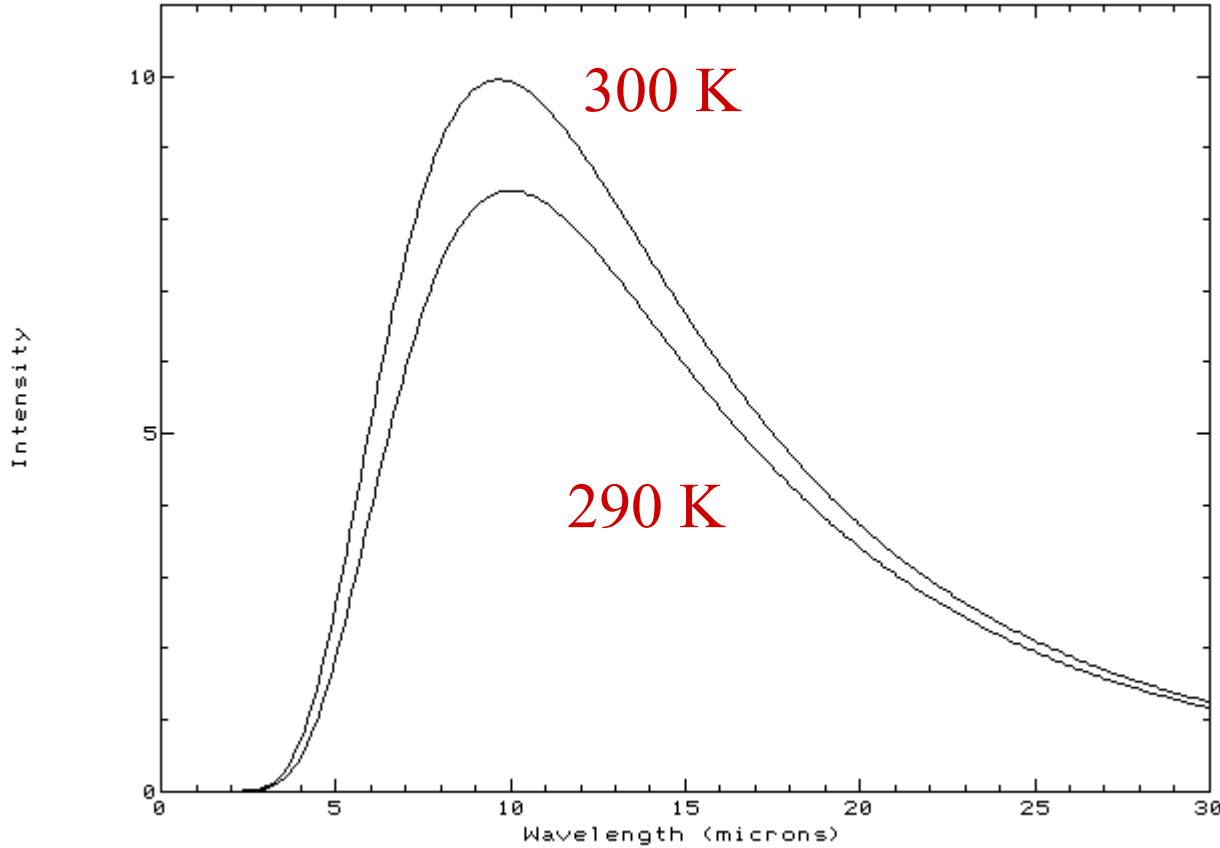
$$T = \left( 459 \text{ W m}^{-2} / (5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}) \right)^{1/4}$$

$$= (8.1 \times 10^9 \text{ K}^4)^{1/4} = 300 \text{ K}$$

$$B(\lambda, T) = \frac{C_1 \lambda^{-5}}{e^{C_2/(\lambda T)} - 1}$$

$$T = \frac{C_2}{\lambda \ln \left[ \left| \frac{C_1}{I \lambda^5} + 1 \right| \right]}$$

# Planck Blackbody Curves

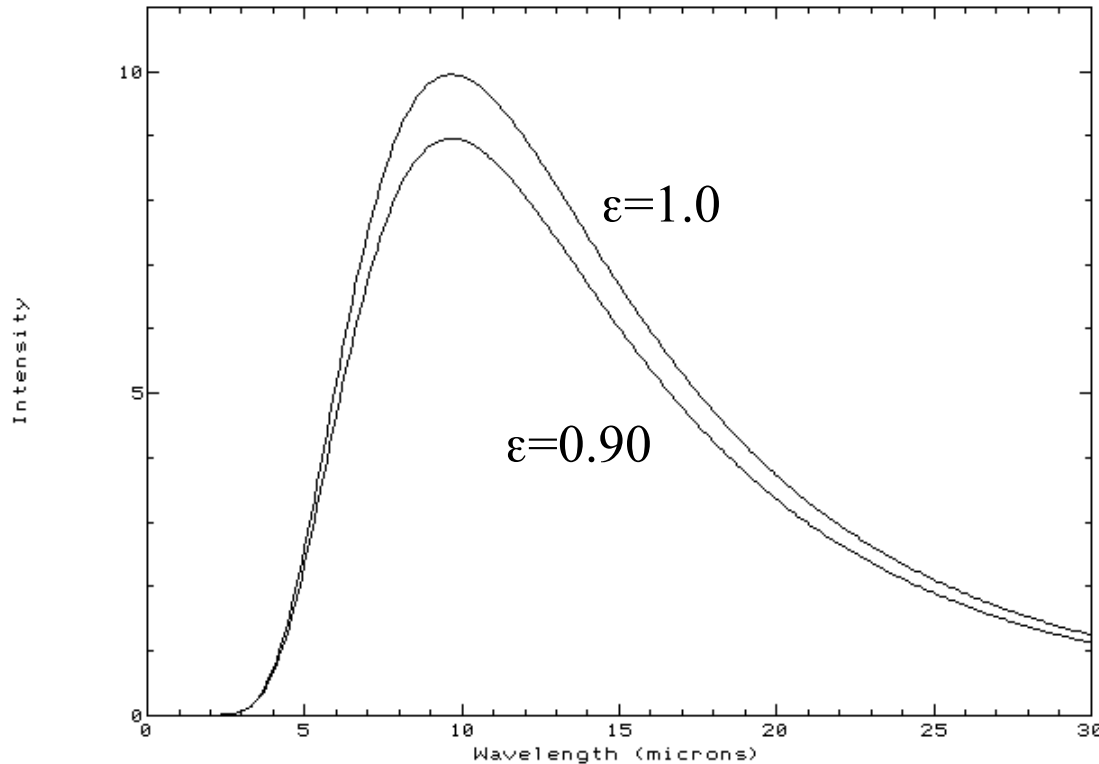


$$B(\lambda, T) = \frac{C_1 \lambda^{-5}}{e^{\frac{C_2}{\lambda T}} - 1}$$

Units of I (or B)

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# Actual Thermal Emission Curves



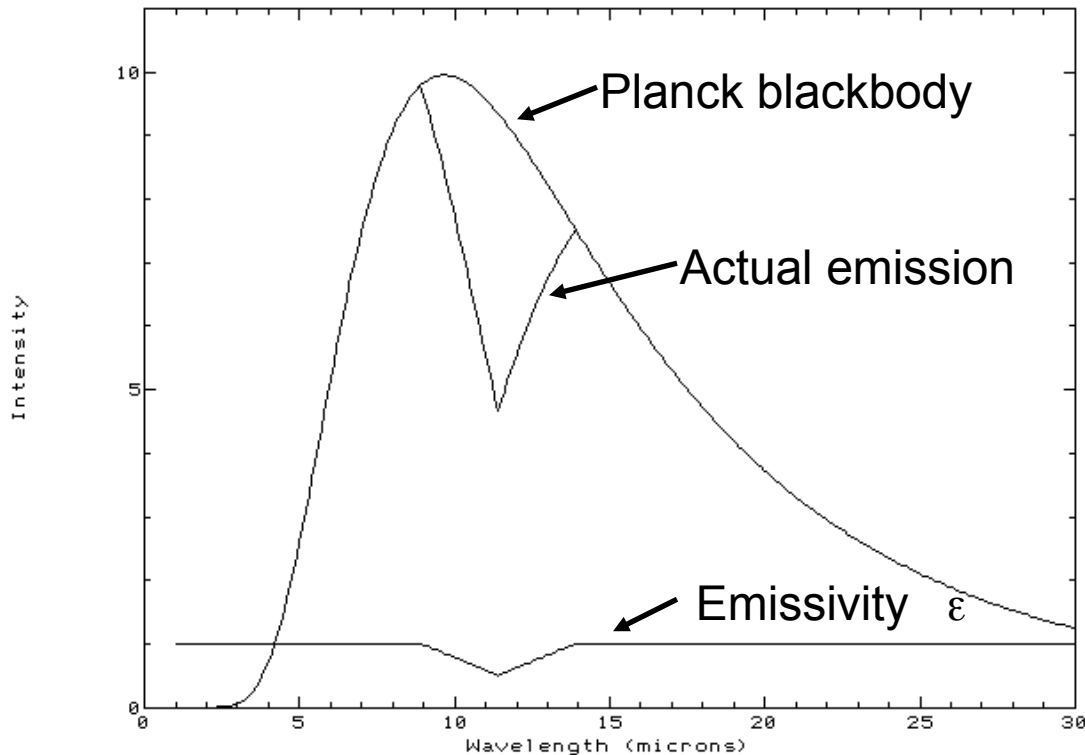
$$B(\lambda, T) = \frac{C_1 \lambda^{-5}}{e^{C_2/(\lambda T)} - 1}$$

$$\epsilon(\lambda) = 1 - r(\lambda)$$

$$\epsilon(\lambda) + r(\lambda) = 1$$

Example where emissivity = 0.9 over all wavelengths

# Actual Thermal Emission Curves



$$B(\lambda, T) = \frac{C_1 \lambda^{-5}}{e^{C_2/(\lambda T)} - 1}$$

$$\varepsilon(\lambda) = 1 - r(\lambda)$$

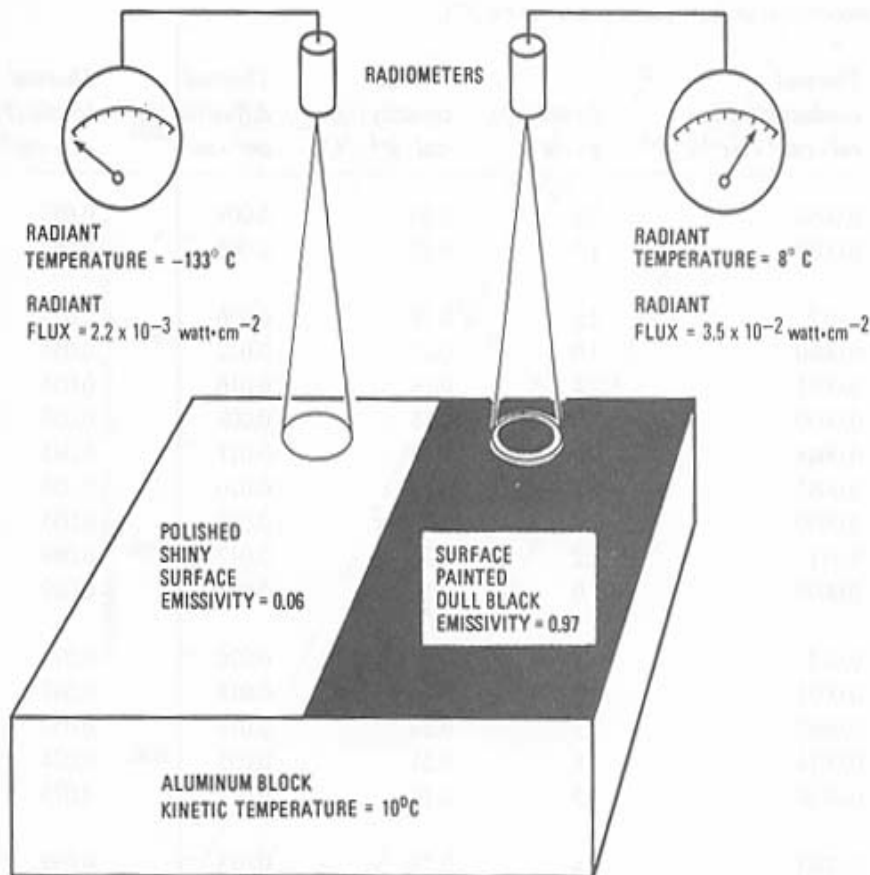
$$\varepsilon(\lambda) + r(\lambda) = 1$$

Example where emissivity drops below 1 from 9 to 14  $\mu\text{m}$

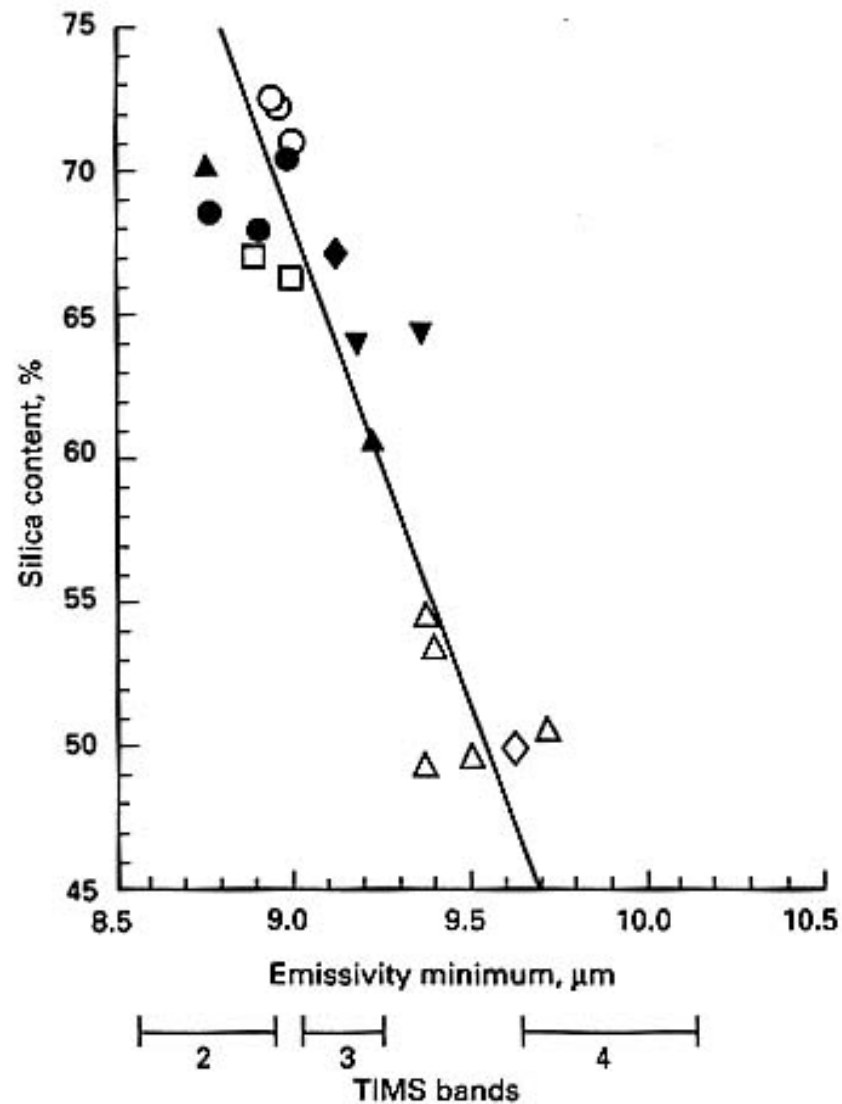
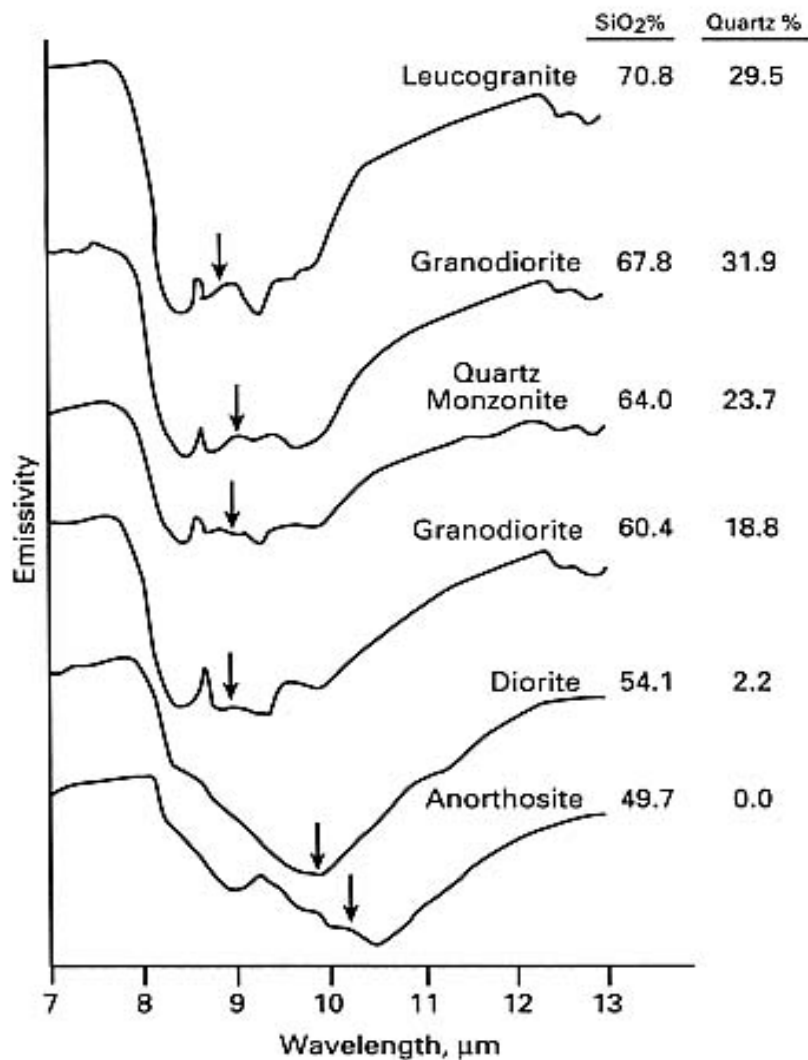


# Emissivity of Materials

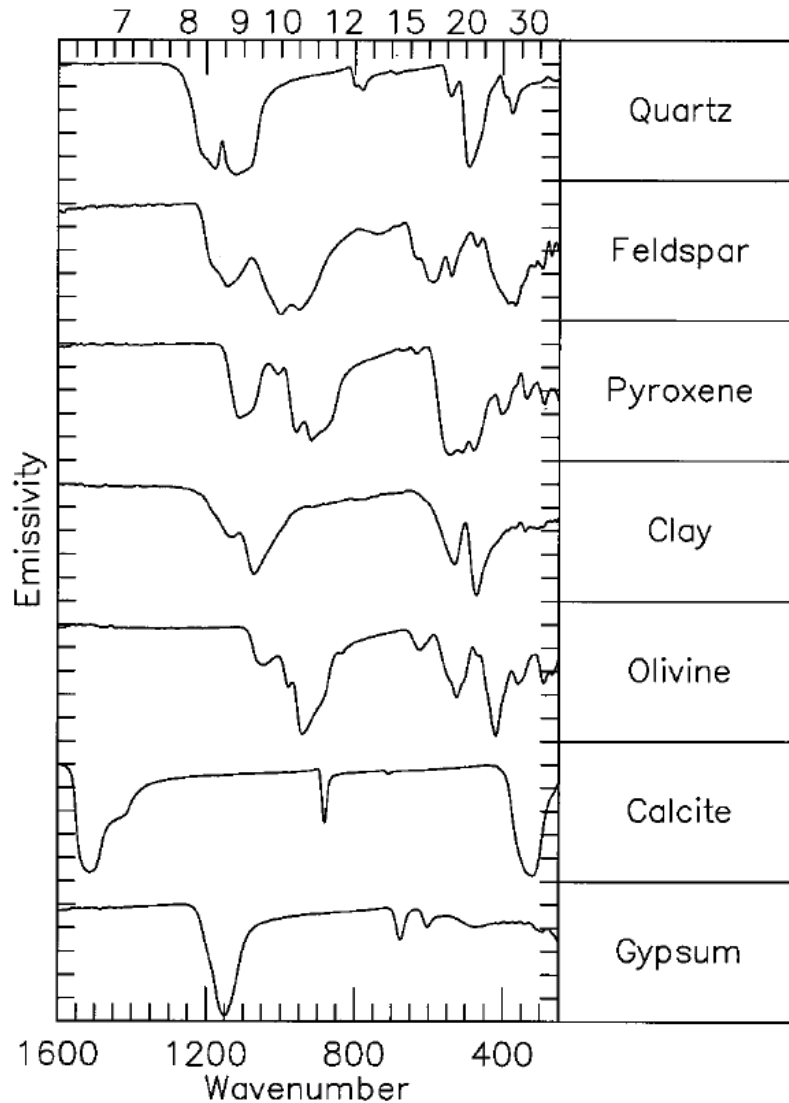
Material	Emissivity, $\epsilon$
water, distilled	0.99
water	0.92 - 0.98
water with petroleum film	0.972
concrete	0.71 - 0.90
asphalt	0.95
tar/stone	0.97
loamy soil, dry	0.92
loamy soil, wet	0.95
soil, sandy	0.90
brick, red and rough	0.93
vegetation, closed canopy	0.98
vegetation, open canopy	0.96
grass	0.97
wood, planed oak	0.90
deciduous forest	0.97 - 0.98
coniferous forest	0.97 - 0.99
stainless steel	0.16
aluminum, foil	0.05
aluminum, polished	0.08
aluminum, paint	0.55
polished metals	0.16 - 0.21
oxidized steel	0.70
granite	0.86
dunite	0.78
basalt, rough	0.95
snow	0.83 - 0.85
paint	0.90 - 0.96
human skin	0.98



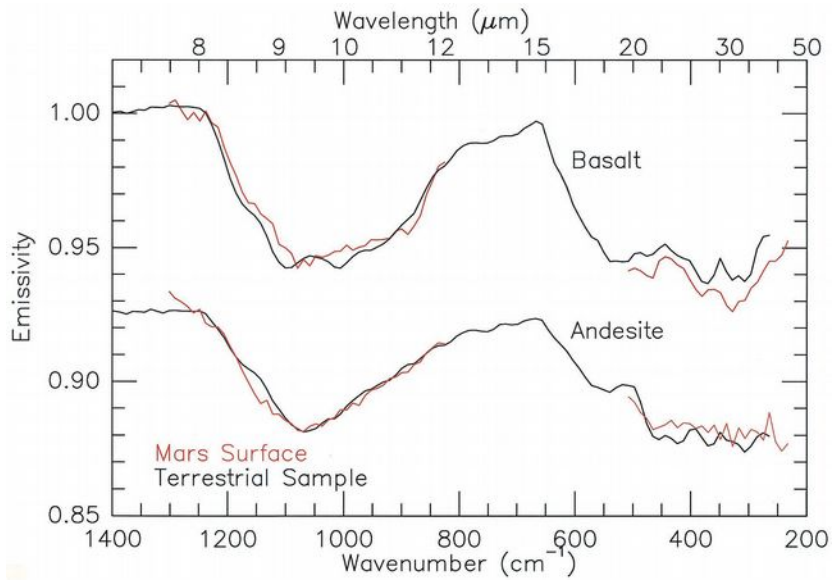
# Emissivity minimum and silica %



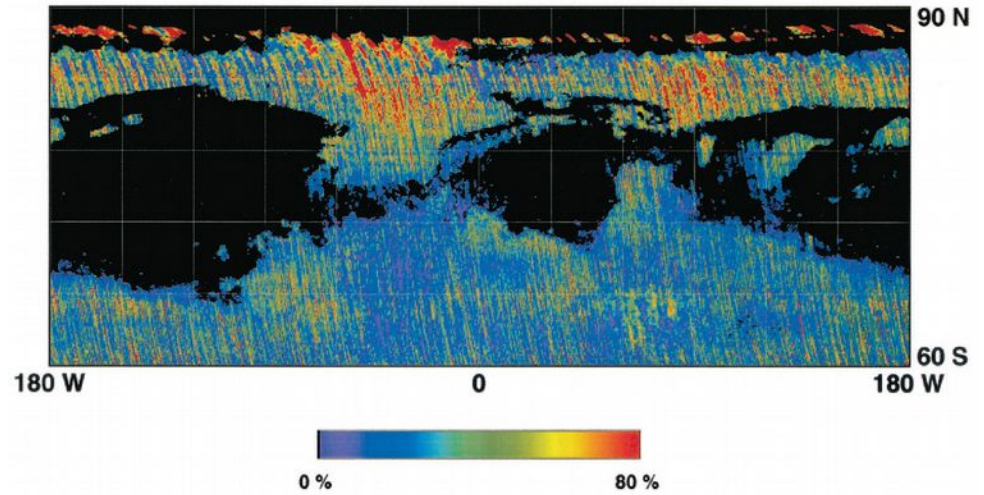
# Emissivity for other minerals



# Mars "TES" Results



## TES Andesite Abundance



## TES Basalt Abundance

