

#1

Using the sandy soil properties and the fact that a thermal wave penetrates roughly a distance

$$\Delta x \approx \sqrt{\frac{k}{\rho c}} \Delta t = \sqrt{k} \sqrt{\Delta t} \quad \text{in time } \Delta t$$

we have

$$k = 0.003 \text{ cm}^2 \text{ s}^{-1} \quad \left(\begin{array}{l} \text{or } 3 \times 10^{-3} \text{ cm}^2 \text{ s}^{-1} \\ \text{or } 3 \times 10^{-7} \text{ m}^2 \text{ s}^{-1} \end{array} \right)$$

If we use $\Delta t = 12 \text{ hr} = 43200 \text{ s}$
 we get $\Delta x = \sqrt{0.003 \text{ cm}^2 \text{ s}^{-1} \cdot 43200 \text{ s}}$
 $= \sqrt{129.6 \text{ cm}^2}$
 $= 11.4 \text{ cm}$

If we had used 24 hr we would get a number $\sqrt{2}$ larger - i.e. 16.1 cm.

Since is just a rough estimate I won't worry about that difference. After all we haven't specified exactly how much of a ΔT we're considering. But the sand must be roughly of no more than the depth where you "see" the underlying bedrock - but deeper than roughly this where you cannot see it.

#2. The amplitude of the T variations will be $\frac{F_0}{\rho \sqrt{\omega}}$ where F_0 is the amplitude of the net flux in and out of the surface (i.e. $F = 136 \text{ W m}^{-2}$), $\omega = \frac{2\pi}{P}$ which is $\frac{2\pi}{24 \text{ hr}} = 7.27 \times 10^{-5} \text{ s}^{-1}$ and $\rho = 0.024 \text{ cal cm}^{-2} \text{ s}^{-1/2} \text{ } ^\circ\text{C}^{-1}$

The 15.9K is the amplitude of the cosine term for T, so the day-night difference is twice this, or 31.8K

To convert to SI units multiply by $4.18 \text{ J/cal} \times (10^2 \text{ cm/m})^2$ (note $1^\circ\text{C} = 1 \text{ K}$)
 so $\rho = 1003 \text{ J m}^{-2} \text{ s}^{-1/2} \text{ K}^{-1}$ giving
 $\frac{F_0}{\rho \sqrt{\omega}} = 136 \text{ W m}^{-2} / (1003 \text{ J m}^{-2} \text{ s}^{-1/2} \text{ K}^{-1} \sqrt{7.27 \times 10^{-5} \text{ s}^{-1}}) = 15.9 \text{ K}$
 note - using $\text{W} = \text{J/s}$ all the other units cancel leaving just K, as they should.