A table of most of the equations we have used (<u>click here for river</u> <u>equations</u>)

Note, the symbols don't translate with some browsers... I am working on the problem

| Basic | | |
|---|--|---|
| Force balance | $\Sigma F = 0$, or $\Sigma F = ma$ | The second form is used if there are any accelerations |
| Hydro or litho static pressure | Ρ = ρ g d | ρ is the material density, and d is the depth of burial |
| Slope stability | | |
| Shear stress, parallel to slope at some depth (perpendicular to slope) | T = ρg d sin α | See <u>notes</u> on slope angles and depths |
| Normal stress, perpendicular to slope | $\sigma = \rho g d \cos \alpha$ | |
| Coefficient of friction | $\mu = tan \phi$ | φ is the internal angle of friction. In the absence of cohesion, φ i s the angle at which a block will slide. |
| Factor of Safety for a slice of a potential failure surface | $FS = (\sigma_{eff} \tan \phi + S) / \tau_s$ | General form of the FS equation. Th e ratio of resisting stresses to driving stresses. Th |

| | | e coefficient of friction is |
|--|---|---|
| | | tan φ or μ. |
| Factor of Safety for a straight dry slope | $FS = (\rho gd \cos\alpha \tan\phi + S) / \rho gd \sin\alpha$ | Where d is the perpendicular to slope depth |
| Water pressure in a 'shallow soiled hillslope' | P _w = ρ _w g d _{wt} cosα | Where d is the 'perpendicula r to slope' depth from the watertable down to the point of interest |
| Effective pressure | $\sigma_{eff} = \sigma_n - P_w$ | Normal stress reduction, as a result of water pressure |
| FS for a wet straight slope, using the 'shallow soil hillslope' approx. for water pressure | $FS = [((\rho_sgd_s + \eta\rho_wgd_{wt}) - \rho_wgd_{wt} \cos\alpha) \\ \cos\alpha \tan\phi + S] / (\rho_sgd_s + \eta\rho_wgd_{wt}) \sin\alpha$ | Note this only applies directly to the specified type of failure |
| After failure, the mass will tend to fall at an acceleration of: | $a = g (sin\alpha - cos\alpha tan\phi)$ | This is just the sum of forces divided by the mass. If the slope doesn't change the acceleration a is a constant. |
| Useful formula for motion, with constant acceleration | $V^2 = 2 a L$ and $2L = a t^2$ | Where v is velocity, L is the slide path length, and t is the time since the |

| | | acceleration (a) was applied |
|--------------------------------------|---|---|
| Stress, Strain and Strain Rate | | |
| Stress | Force per area | This is a tensorial quantity, with magnitude and two directions |
| Strain τφ | Change of length with length. Example: a normal strain component (only for very small Δx) $\epsilon_{xx} = \Delta x / (original length in x)$ A shear strain is more complex $\epsilon_{xy} = \frac{1}{2} [\Delta y / (original x) + \Delta x / (original y)]$ | Although dimensionles s, this is also a tensor! |
| Strain rate | Calculation of shear strain rate in a fluid $\varepsilon^{o}_{xy} = \frac{1}{2} [\Delta V_y / \Delta x + \Delta V_x / \Delta y]$ | The shear strain rate is determined by gradients in the velocities |
| Debris flow equations | | |
| | A page of velocity equations here | |
| Two useful velocity equations | $V = (2 g z)^{\frac{1}{2}}$ $V = (g (R/W) z)^{\frac{1}{2}}$ | Where z is the superelevatio n. The first can be used for water piling up against an obstacle, the 2 nd for water going around a bend of radius R and flow width W. |

| Convolution for Shallow Soiled Hillslope approximatio n, and other distributed input to point output processes. | $d_{w.t.}(t,X) = \frac{1}{K_{sat}\sin\alpha} \begin{cases} \sum_{\tau=t}^{\tau=t} R(t-\tau)\Delta t \\ \tau = \frac{\Delta x}{K_{sat}\sin\alpha} \end{cases}$ $\Delta \tau = \frac{\Delta x}{K_{sat}\sin\alpha} $ $t_{start} = t - (\frac{X}{K_{sat}\sin\alpha})$ | This gives the water table at time 't', at some distance X downslope. The sum runs from sometime in the past (see note below) |
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| | | thru the sum) is given by $\Delta \tau$. This form only works for constant slope and water velocity. Note, the start time of the sum, is the time in the past when water that is passing the point you are interested in, fell on the top of the hill. In other words: τ (lower limit) is [slope length/water velocity], note this is a [past] time. |